

K.C.S.E YEAR 2010 PAPER 1 MARKING

$$1. = \frac{-2(5+3) - 9 \div 3 + 5}{-3 \times -5 + (-2) \times 4} = \frac{-14}{7}$$

$$= -2$$

2. Total fraction:

$$\frac{3}{8} + \frac{2}{5} = \frac{31}{40}$$

$$\text{Remaining fraction} = 1 - \frac{31}{40}$$

$$= \frac{9}{40}$$

$$\text{original amount} = \text{sh.}12330 \times \frac{40}{9}$$

$$= \text{sh.}54800$$

$$\text{Tatu's fees} = \text{sh.} \frac{2}{5} \times 54800$$

$$= \text{sh.}21920$$

3. Gradient (perpendicular) =  $-\frac{1}{2}$

$$\frac{y+2}{x-3} = -\frac{1}{2}$$

$$y = -\frac{1}{2}x - \frac{1}{2}$$

4. let the distance be d km

$$\frac{d}{75} \text{ and } \frac{d}{95}$$

$$\therefore \frac{d}{75} - \frac{d}{95} = \frac{20}{60}$$

$$d = \underline{118.75\text{km}}$$

5. Let odd integers be:

$$x, (x+2), (x+2+2)$$

$$x + (x+2) + (x+2+2) > 219$$

$$3x > 213$$

$$x = 71$$

The numbers are 73, 75, 77

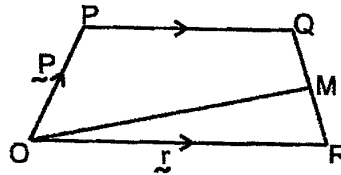
6. (a) sh.77.24 × 100,000

$$= \text{sh.}7,724,000$$

(b)  $\frac{\text{sh.}77.24 \times 10000}{122.27}$

$$= \text{£}63172$$

7



$$\underline{OQ} = -\underline{r} + \underline{p} + \frac{1}{3}\underline{r}$$

$$= \underline{p} - \frac{2}{3}\underline{r}$$

$$\underline{OM} = \underline{r} + \frac{1}{2}(\underline{p} - \frac{2}{3}\underline{r})$$

$$= \frac{2}{3}\underline{r} + \frac{1}{2}\underline{p}$$

8.

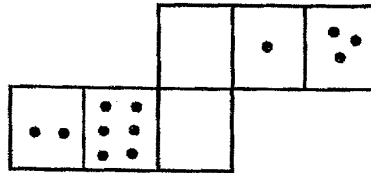
$$27^3 \times \left(\frac{81}{16}\right)^{-4} = (3^3)^3 \times \left(\frac{3^4}{2^4}\right)^{-4}$$

$$= 3^9 \times \left(\frac{3}{2}\right)^{-4}$$

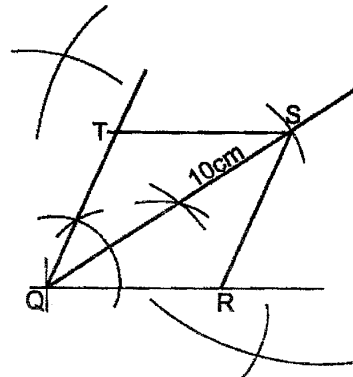
$$= 3^9 \times \frac{2}{3}$$

$$= 6$$

9.



10.



<TQR = 60°; QS = 10cm and bisects <TQR

Mediator (⊥ or bisector) of QS drawn or

<RSQ = <QST = <RQS = 30°

✓ Rhombus completed

11. No of oranges for Friday  
 $1948 - (750 + 750 + 240)$   
 $= 208$   
 No of oranges for Saturday  
 $208 + 560 = 768$   
 $\therefore$  Amount = sh.8  $\times$  768  
 $=$  sh.6144

12. 
$$\frac{x^2 + x - 4xy - 4y}{(x+1)(4y^2 - xy)} = \frac{x(x+1) - 4y(x+1)}{(x+1)(y)(4y-x)}$$

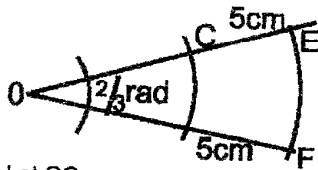
$$= \frac{(x-4y)(x+1)}{(x+1)(-y)(x-4y)}$$

$$= -\frac{1}{y}$$

13.  $\sin 3\theta = \cos 2\theta$   
 $\therefore \sin 3\theta = \sin (90^\circ - 2\theta)$   
 $\therefore 3\theta = 90^\circ - 2\theta$   
 $5\theta = 90$   
 $\theta = 18^\circ$

14.  $2\pi r^2 + 2\pi rh = 154$   
 $r = h$   
 $2\pi r^2 + 2\pi r^2 = 154$   
 $4\pi r^2 = 154$   
 $r = \sqrt{\frac{154}{4 \times 3.142}}$   
 $r = 3.500$   
 $\therefore$  diameter =  $2r = 3.500 \times 2$   
 $= 7.00(2dp)$

15.



Let  $OC = r$   
 $\therefore CD = \frac{2}{3}r$  and  $EF = \frac{2}{3}(r+5)$

$\frac{2}{3}r + \frac{2}{3}(r+5) + 5 + 5 = 24$

$\frac{4}{3}r = 10\frac{2}{3}$

$r = 8$

16.

Total number of seedlings  
 $(5 \times 1) + (10 \times 3) + (15 \times 1) + (20 \times 4) + (30 \times 1) + (10 \times 2)$   
 $= 5 + 30 + 15 + 80 + 30 + 20 = 180$   
 % of height (h) :  $23 \leq h < 27$   
 $= \left(\frac{30+15}{180}\right) \times 100$   
 $= 25\%$

17. (a) Total sales = sh.360  $\times$  500  
 $=$  sh.180,000

Commission = sh.(180,000 - 100,000)  $\times$   $\frac{2}{3}$   
 $=$  sh.1600  
 Total earnings = sh.(12,000 + 1600)  
 $=$  13600

- (b) (i) New salary = sh.(12000 +  $12000 \times \frac{10}{100}$ )  
 $=$  sh. 13200  
 Commission paid = sh.(17,600 - 13,200)  
 $=$  sh.4400  
 Commission is paid on sh.4400  $\times$   $\frac{100}{2}$   
 $=$  220,000  
 Total sales = sh.220,000 + 100,000  
 $=$  320,000/=

(ii) No of handbags sold =  $\frac{320,000}{500}$   
 $=$  640

18. (a) (i) Internal volume of box =  $150 \times 80 \times 40 \text{ cm}^3$   
 $= 480,000 \text{ cm}^3$   
 External volume of box =  $152 \times 82 \times 42 \text{ cm}^3$   
 $= 523488 \text{ cm}^3$   
 $\therefore$  Volume of wood =  $(523488 - 480,000) \text{ cm}^3$   
 $= 43488 \text{ cm}^3$

(ii) Mass of box =  $\frac{43488 \times 0.6}{1000}$   
 $= 26092.8$   
 $= 26.1 \text{ kg}$

(b) (i) No of tins =  $\frac{150}{10} \times \frac{80}{10} \times \frac{40}{10}$   
 $= 240$

(ii) Total mass =  $26.1 + \left(\frac{240 \times 120}{1000}\right)$   
 $= 54.9 \text{ kg}$

19. (a) Det | 45 - 42 | = 3

Inverse  $A^{-1} = \frac{1}{3} \begin{pmatrix} 9 & -6 \\ -7 & 5 \end{pmatrix}$

(b)  $\begin{pmatrix} 5 & 6 \\ 6 & 9 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2440 \\ 3560 \end{pmatrix}$

(ii)

$\frac{1}{3} \begin{pmatrix} 9 & -6 \\ -7 & 5 \end{pmatrix} \begin{pmatrix} 5 & 6 \\ 6 & 9 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 3 & -2 \\ -7 & 5 \end{pmatrix} \begin{pmatrix} 2440 \\ 3560 \end{pmatrix}$

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 3 \times 2440 - 2 \times 3560 \\ -\frac{7}{3} \times 2440 + \frac{5}{3} \times 3560 \end{pmatrix}$$

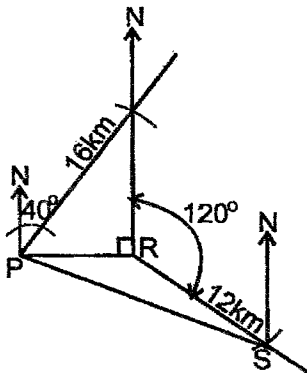
$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 200 \\ 240 \end{pmatrix}$$

$$\therefore x=200 ; y=240$$

$$(c) \text{ Total cost of books } = (36 \times 200) + (50 \times 240) = 19200$$

$$\begin{aligned} \text{Total cost with discount} &= \frac{36 \times 200 \times 95}{100} + \frac{50 \times 240 \times 92}{100} \\ &= 17880 \\ \% \text{ discount} &= \frac{19200 - 17880}{19200} \times 100 \\ &= 6.875\% \end{aligned}$$

20. Given scale: 1 cm to 2 km



$$(b) (i) \text{ Distance of P from S } = 10.8 \pm 0.1 \text{ cm} = 21.6 \text{ km}$$

$$(ii) \angle PSN = 74 \pm 1^\circ$$

$$\text{Bearing of P from S} = 286 \pm 1^\circ$$

$$(c) \text{ Area of } \Delta PQR = \frac{1}{2} \times 10.2 \times 12.2 = 62.22 \text{ km}^2$$

$$\text{Area of } \Delta PRS = \frac{1}{2} \times 10.2 \times 12 \sin 150^\circ = 30.6 \text{ km}^2$$

$$\begin{aligned} \text{Area of ranch PQRS} &= 62.22 + 30.6 \\ &= 92.82 \text{ km}^2 \end{aligned}$$

$$21. (a) (i) A \text{ takes } \frac{180}{x+10}$$

$$(ii) B \text{ takes } \frac{180}{x}$$

$$(b) \frac{180}{x} - \frac{180}{x+10} = \frac{3}{2}$$

$$180(x+10) - 180x = \frac{3}{2}x(x+10)$$

$$360x + 3600 - 360x = 3x^2 + 30x$$

$$x^2 + 10x - 1200 = 0$$

$$(x-30)(x+40) = 0$$

$$x = 30 \text{ or } x = -40$$

$$\text{Speed of A} = 30 + 10 = 40$$

$$(c) \text{ Time taken by A} = \frac{48}{40} \times 60 = 72 \text{ min}$$

$$\text{Time taken by B} = \frac{48}{30} \times 60 = 96 \text{ min}$$

$$\text{Time for B} = 96 - 10 = 86 \text{ min}$$

$$86 - 72 = 14 \text{ min}$$

22. (a) (i) Reflection in the line PR or ER  
Or PER

(ii) Enlargement centre E  
Scale factor - 1

(iii) Rotation about pt R  
Through  $90^\circ$   
Clockwise

$$(c) R \rightarrow S$$

$$C \rightarrow A$$

$$(ii) R \rightarrow Q$$

$$C \rightarrow E$$

23. Modal frequency = 8

(b)

No of kg of meat	Fre. (f)	Mid pts (x)	fx	cf
1 - 5	2	3	6	2
6 - 10	3	8	24	5
11 - 15	6	13	78	11
16 - 20	8	18	144	19
21 - 25	3	23	69	22
26 - 30	2	28	56	24
31 - 35	1	33	33	25
	$\Sigma f = 25$		$\Sigma fx = 410$	

$$\text{Mean} = \frac{410}{25} = 16.4$$

(d) 2, 5, 11, 19, 22, 24, 25

$$\text{Median} = 15.5 + \frac{12.5 - 11}{8} \times 5$$

$$= 15.5 + \frac{1.5}{8} \times 5$$

$$= 16.4375$$

24. (a) (i) Area of base  $x^2$   
Or Area of sides =  $4xh$   
 $x^2 + 4xh = 432$

$$h = \frac{432 - x^2}{4x}$$

(iii) Volume =  $x^2h$   
 $= x^2(432 - x^2)$

(b) (i) Volume (v) =  $108x - \frac{1}{4}x^3$

$$\frac{dv}{dx} = 108 - \frac{3}{4}x^2$$

$$108 - \frac{3}{4}x^2 = 0$$

$$x = 12$$

(ii) Vol =  $108x - \frac{1}{4}x^3$   
 $= (108 \times 12) - \frac{1}{4} \times 12^3$   
 $= 864 \text{cm}^3$