3.4.2 Mathematics Alt.B Paper 2 (122/2)

SECTION I (50 marks)

Answer all the questions in this section in the spaces provided.

1. Evaluate 190.1 \times 30, correct to 3 significant figures.

(2 marks)

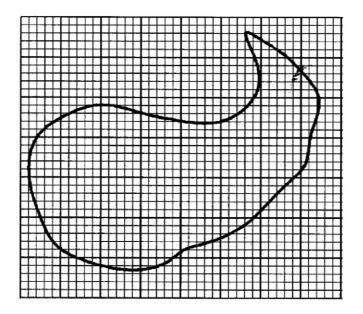
2. Find the sum of the first 10 terms in the Geometric Progression 3, 6, 12, ...

(3 marks)

3. Given that 5, x, 35 and 84 are in proportion, find the value of x.

(3 marks)

- 4. The base of a triangle is 3 cm longer than its height and its area is 35 cm². Determine the height and base of the triangle. (4 marks)
- 5. The figure below is a map of a piece of land on a grid of 1 cm squares.



Estimate the area of the map in square centimetres.

(3 marks)

- 6. A chord of a circle, radius 5 cm, subtends an angle of 30° at the centre of the circle. Determine the length of the chord, correct to 2 decimal places. (3 marks)
- 7. The extension (E), in cm, of a rubber band when pulled by a force (F) was found experimentally and recorded as shown in the table below:

Force (F)	0	2	4	6	8
Extension (E) cm	0	3	6	9	12

(a) On the grid provided, draw a graph of extension(E) against force(F).

(2 marks)

(b) Use the graph to determine the extension when the force is 7 units.

(1 mark)

8. The position of towns M and N are $M(0^{\circ}, 51^{\circ}W)$ and $N(0^{\circ}, 37^{\circ}E)$. Find the distance between the two towns in kilometres, correct to one decimal place.

(Take the radius of the earth as 6370 km and
$$\pi = \frac{22}{7}$$
)

(3 marks)

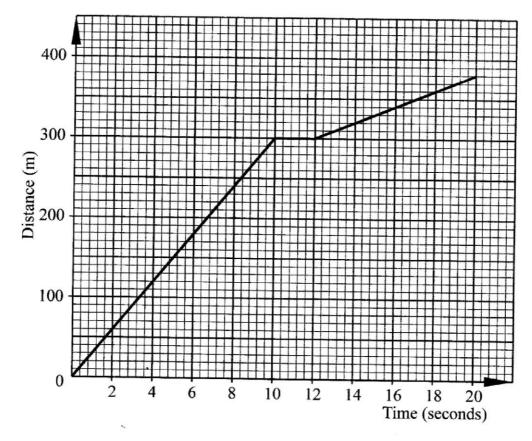
9. The table below shows the values of $y = 2\sin(\theta + 30^\circ)$ for $0^\circ \le \theta \le 360^\circ$.

θ	0°	30°	60°	90°	120°	150°	180°	210°	240°	270°	300°	330°	360°
$y = 2\sin(\theta + 30^{\circ})$	1	1.7	2	1.7	1	0	-1	-1.7	-2	-1.7	-1	0	1

- (a) On the grid provided below, draw the graph of $y = 2\sin(\theta + 30^\circ)$ for $0^\circ \le \theta \le 360^\circ$. Use 1 cm for 30° on the x-axis and 2 cm for one unit on the y-axis. (3 marks)
- (b) Use the graph to determine the value of y when $\theta = 162^{\circ}$.

(1 mark)

10. The figure below represents the distance covered by a car within a given period of time.



Find the average speed of the car in kilometres per hour.

(3 marks)

11. Kitonga deposited Ksh 50 000 in a bank which paid compound interest at the rate of 10% per annum. Find the compound interest accrued by the end of the fourth year. (3 marks)

The number of different vehicles allowed through a road block was recorded as follows: 12.

Type of vehicles	Cars	Lorries	Pick-ups	Buses	Tankers
No. of vehicles	59	35	26	47	13

Represent the above data in a pie chart.

(3 marks)

- Somi bought 2 pencils and 3 rubbers for Ksh 60 from a certain shop. Miheso bought 1 pencil 13. and 2 rubbers for Ksh 35 from the same shop. Find the price of one pencil and that of one rubber. (3 marks)
- Find a matrix which, when multiplied by matrix $\mathbf{M} = \begin{pmatrix} 3 & 2 \\ 7 & 5 \end{pmatrix}$ gives the identity 14. (a) (2 marks)
 - Given that $N = \begin{pmatrix} x & 2 \\ 6 & 4 \end{pmatrix}$ is a singular matrix, find the value of x. (2 marks)
- A square QRST with vertices Q(1,1), R(3,1), S(3,3) and T(1,3) is transformed by the matrix 15. $\begin{pmatrix} 3 & 1 \\ 0 & 2 \end{pmatrix}$ to Q'R'S'T'. Find:
 - (a) the area of square QRST;

(2 marks)

(b) the area of image Q'R'S'T'.

(2 marks)

Given that $\mathbf{p} = 6\mathbf{i} + 2\mathbf{j}$, determine the magnitude of \mathbf{p} , correct to 2 decimal places. 16. (2 marks)

SECTION II (50 marks)

Answer any five questions from this section in the spaces provided.

- The second term of an arithmetic progression(AP) and fourth term of a geometric 17. progression(GP) are each 80. The sixth terms of the AP and GP are each 320.
 - (a) Find:

the first term and the common differences of the AP. (i)

(2 marks)

(ii) the first term and the common ratio of the GP.

(2 marks)

Determine the 20th term of the AP. (b)

(2 marks)

Determine the difference between the sum of the first 12 terms of the GP and the sum of (c) the first 12 terms of the AP. (4 marks) 18. (a) (i) Complete the table below for the values of $y = x^2 - x - 6$ for $-3 \le x \le 4$. (2 marks)

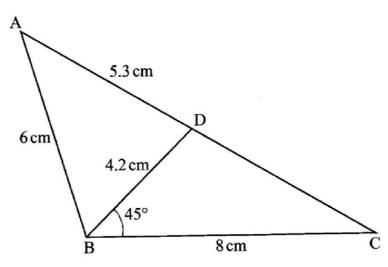
x	-3	-2	-1	0	1	2	3	4
$y = x^2 - x - 6$								

(ii) Find y when
$$x = \frac{1}{2}$$
. (1 mark)

- (b) On the grid provided, draw a graph of $y = x^2 x 6$ for $-3 \le x \le 4$. (3 marks)
- (c) On the same grid, draw line $y = \frac{-3}{2}x + 1$ and hence solve the equation $x^2 x 6 = \frac{-3}{2}x + 1$. (4 marks)
- 19. The marked price of a wall unit was Ksh 50 000. The price on hire purchase (HP) terms was 175% of the marked price.
 - (a) A customer bought the wall unit in cash and was offered 10% discount. Find the amount of money the customer paid for the wall unit. (2 marks)
 - (b) A second customer decided to purchase a similar wall unit on HP terms.
 - (i) Determine the HP price. (2 marks)
 - (ii) The customer paid 20% of the HP price as deposit and was to pay the balance in 28 equal monthly instalments. Find the amount of each monthly instalment.

 (3 marks)
 - (c) A third customer bought a similar wall unit in cash by taking a loan equal to the marked price. The loan was to be repaid in 15 months and the bank charged interest at the rate of 4% compounded monthly.
 - (i) Find, correct to the nearest shilling, the amount of money the third customer paid the bank. (2 marks)
 - (ii) Find the amount of money the third customer spent more than the marked price.
 (1 mark)

20. The figure below shows triangle ABC in which AB = 6 cm, BC = 8 cm, BD = 4.2 cm and AD = 5.3 cm. Angle $CBD = 45^{\circ}$.



Calculate, correct to one decimal place:

(a) the length of CD;

(3 marks)

(b) size of angle ABD;

(3 marks)

(c) size of angle BCD;

(2 marks)

(d) area of triangle ABD.

(2 marks)

21. Mawira, a poultry farmer carried out the following transactions during the month of February 2017:

February 1: Had Ksh 10000 carried forward from January 2017

3: Bought 2 bags poultry feed @Ksh 1250

7: Paid Ksh 750 for water

11: Bought materials for construction for Ksh 1900

13: Received Ksh 12000 from sale of broilers

17: Sold 500 eggs at Ksh 8 each

21: Paid wages to 2 casuals at Ksh 1750 each

24: Sold chicks for Ksh 5 000

25: Paid Ksh 1 300 for electricity

26: Sold 30 layers at Ksh 500 each

28: Bought incubator for Ksh 12 500

Prepare a single column cash book for Mawira's transactions and balance it as at 1st March (10 marks)

22. The table below shows the marks of 50 candidates in a test.

Marks	1–10	11–20	21-30	31–40	41–50	51–60	61–70	71–80	81–90	91–100
Frequency	2	4	5	8	11	9	5	3	2	1

(a) Draw a cumulative frequency curve for the data.

(5 marks)

- (b) Use the graph to determine:
 - (i) the median mark;

(2 marks)

(ii) the percentage of students who scored above 64%.

(3 marks)

- 23. Two boxes B and C contain identical balls except for the colour. Box B contains 5 violet balls and 3 green balls. Box C contains 3 violet balls and 4 green balls.
 - (a) A ball is drawn at random from each box. Find the probability that both balls are of the same colour. (4 marks)
 - (b) Two balls were drawn at random from each box, one ball at a time without replacement. Find the probability that:
 - (i) the two balls drawn from box B or box C are violet;

(4 marks)

(ii) all the four balls drawn are violet.

(2 marks)

- 24. The vertices of a triangle ABC are A(2, 2), B(5, 3) and C(3, 5).
 - (a) Find the vertices of Δ A'B'C' the image of Δ ABC under the transformation represented by the matrix $\begin{pmatrix} 0 & 2 \\ 2 & 0 \end{pmatrix}$. (2 marks)
 - (b) Triangle ABC is mapped onto Δ A"B"C" whose vertices are A"(-2, 2), B"(-5, 3) and C"(-3, 5). Find the matrix of this transformation. (4 marks)
 - (c) Triangle ABC undergoes two successive transformations $\mathbf{PQ} = \begin{pmatrix} 1 & 0 \\ 2 & 1 \end{pmatrix} \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$. Determine the vertices of Δ A"B"C", the image of Δ ABC, under the combined transformation. (4 marks)