

# KAPSABET HIGH SCHOOL

121/1

(Kenya Certificate of Secondary Education)

Paper 1



## INTERNAL MOCK EXAM MATHEMATICS

ALT A

Dec. 2020– 2 ½ Hours

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# MARKING SCHEME

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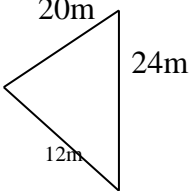
### Instructions to candidates

- (a) Write your name, admission number and stream in the spaces provided above.
  - (b) Sign and write the date of examination in the spaces provided above.
  - (c) This paper consists of **two** sections: **Section I** and **Section II**.
  - (d) Answer **all** the questions in **Section I** and only **five** questions from **Section II**.
  - (e) **Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.**
  - (f) Marks may be given for correct working even if the answer is wrong.
  - (g) **Non-programmable** silent electronic calculators **and** KNEC Mathematical tables may be used, except where stated otherwise.
  - (h) **Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.**
  - (i) Candidates should answer the questions in **English**
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**SECTION A ( 50 marks)**

1.	$\frac{42}{-14} - \frac{-96 - 12}{-9 \times 3}$ $\frac{42}{-14} - \frac{-108}{-27}$ <p>-3 -4</p> <p>-7</p>	<p>M1</p> <p>M1</p> <p>A1</p>	Simplification with single numerator and denominator
2.	<p align="center"><i>LCM 2 X 3 X 5</i></p> <p align="center">30minutes</p> $\frac{30}{3} + \frac{30}{5} + \frac{30}{6}$ <p>21 customers</p> $\frac{210}{21} \times 30$ <p>300minutes</p>	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>4</p>	
3.	$(2^{y+2y} \times 5^{3y})^{1/3}$ $(2^{3y} \times 5^{3y})^{1/3}$ $2^y \times 5^y$ $(2 \times 5)^y$ $10^y$	<p>M1</p> <p>A1</p> <p>2</p>	For removal of cube root
4.	$\frac{2.4}{100} \times 200,000$ <p>Sh. 4800</p> <p>2.4 + 1.2</p> $\frac{3.6}{100} \times 180,000$ <p>Sh. 6480</p> <p>6480 + 4800</p> <p>Sh. 11,280.</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>3</p>	For calculation of exterior angle.
5.	<p>Exterior angle</p> $\frac{2}{9} \times 180^0$ $40^0$ $n = \frac{360}{40}$ <p>9sides</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>3</p>	

6.	$n+n+2+n+4+n+6 > 248$ $4n+12 > 248$ $4n > 236$ $n > 59$  60,62,64,66	M1  A1  B1 3	
7.	$\frac{L}{\sin 60^\circ} = 2 \times 8$ $L = 16 \sin 60^\circ$ $L = 13.86 \text{ cm}$	M1  A1 2	
8.	$\begin{pmatrix} 0 & 1 \\ 2 & x \end{pmatrix} \begin{pmatrix} -\frac{3}{2} & -\frac{1}{2} \\ x & x-2 \end{pmatrix}$ $\begin{pmatrix} x & x-2 \\ -3+x2 & -1+x(x-2) \end{pmatrix}$ $x(-1+x^2-2x) - (-3+x^2)(x-2) = 0$ $-x+x^3-2x^2 - (-3x+6+x^3-2x^2) = 0$ $-x+x^3-2x^2+3x-6-x^3+2x^2 = 0$ $2x-6=0$ $2x=6$ $X=3$	B1 M1 M1 A1 4	For the product of the matrices For determinant and equating it to 0 For $\sqrt{\text{removal of brackets}}$
9.	Long diff $120^\circ + 143^\circ = 263^\circ$ Minir arc $360^\circ - 263^\circ = 97^\circ$ $97^\circ \times 60 \cos x = 5068$ $X = 29.45^\circ$ $= 29.45^0 \text{ s}$	B1 B1 M1  A1  4	For $263^0$ For $97^0$
10.	$3c + 4s = 648 \dots x1$ $5c = 2s = 456 \dots x2$  $3c + 4s = 648$ $10c - 4s = 912$ <hr/> $13c = 1560$ 1 cup costs sh. 120 1 spoon costs sh. 72	B1  M1  A1  3	For the two equations $\sqrt{\text{attempt to eliminate one unknown}}$
11.	1,2,4,4,5,6,6,7,7,8,9 1,2,4,4,5,6 $Q1 = \frac{4+4}{2}$ 4	B1	For $Q_1=4$

	6,6,7,7,8,9 $Q_3 = \frac{7+7}{2} = 7$ $QD = \frac{7-4}{2} = 1.5$	B1 B1 3	For $Q_3=7$
12.	3,133,792+5293476+7672598+4257348 20,357,214 20360000 20,357,214 – 20360000  - 2786	B1 M1 A1 3	Corrected to the nearest 10,000
13.			
14.	$\frac{x}{10} + \frac{x}{12} = 1\frac{5}{6}$ $\frac{x}{10} + \frac{x}{12} = \frac{11}{6}$ 6x+5x=110 11x=110 X=10km	M1 M1 A1 3	For total time taken  Removal of denominator
15.	y=-6x-p qy + 4x -10=0 $y = \frac{-4}{q}x + \frac{10}{q}$ -6 x -4/q=-1 24/q =-1 Q=-24 -2=6x4-p -2=-24-p P=-22	M1 A1 M1 A1 4	
16.	$\frac{3}{14} \times 56 \times 12m$ $\frac{5}{14} \times 56 \times 20m$ $\frac{6}{14} \times 56 \times 24m$ $\cos \theta = \frac{12^2 + 24^2 - 20^2}{2 \times 12 \times 24}$  $\theta = 56.25^\circ$	 M1 M1 A1 3	For $\frac{3}{14} \times 56, \frac{5}{14} \times 56, \frac{6}{14} \times 56$  For cosine rule or equivalent

<b>SECTION B</b>			
17.	a.) $(3x+9)(x-3)=648$ $3x^2-675=0$  b.) $3x^2-675=0$ $X^2-225=0$ $(x-15)(x+15)=0$ $x-15=0$ $x=15m$ 54m by 12m  c.) A.s.f=648:2592 1:4 l.s.f = 1:2 54x2= 108m 12x2 =24m	M1 A1  M1 M1  A1 B1  M1 A1 B1 A1 B1	For 108m and 24m
18.	a.) $\Delta PQR$  b.) (i) <i>plotting of points of line <math>y = x + 1</math></i>  (ii) One point correctly reflected  c.) One point correctly rotated through $-90^0$ about (0,0)  <div style="text-align: center;"> <math display="block">\left. \begin{array}{l} T \quad P'' \quad P''' \\ \begin{pmatrix} 2 \\ 3 \end{pmatrix} + \begin{pmatrix} -2 \\ -1 \end{pmatrix} = \begin{pmatrix} 0 \\ 2 \end{pmatrix} \\ Q'' \quad Q''' \\ \begin{pmatrix} 2 \\ 3 \end{pmatrix} + \begin{pmatrix} 0 \\ -1 \end{pmatrix} = \begin{pmatrix} 0 \\ -1 \end{pmatrix} \\ R'' \quad R''' \\ \begin{pmatrix} 2 \\ 3 \end{pmatrix} + \begin{pmatrix} 0 \\ -3 \end{pmatrix} = \begin{pmatrix} 0 \\ -3 \end{pmatrix} \end{array} \right\}</math> </div> $P'''(0,2) \quad Q'''(0,-1) \quad R'''(0,-3)$  i.) $P''' Q''' R'''$	B1  P1  L1  B1  B1  B1  B1  M1  A1  B1  10	$\sqrt{\text{drawn}}$  At least two points plotted.  Line $y=x+1$ correctly drawn.  $\Delta P^I Q^I R^I$ correctly drawn.  $\Delta P^{II} Q^{II} R^{II}$ correctly drawn.  $\sqrt{\text{attempt to find } P'''} \\ Q''' R'''} \\ \sqrt{\text{co-ordinates}}$  $\Delta P''' Q''' R'''$ $R''' \sqrt{\text{drawn}}$

19.	<p>a.) <math>\frac{120}{20} = \frac{R}{14}</math>  <math>6 = \frac{R}{14}</math>  <math>R = 84\text{cm}</math></p> <p>b.) <math>L^2 = 120^2 + 84^2</math>  <math>L = \sqrt{120^2 + 84^2}</math>  <math>= 146.5\text{cm}</math>  <math>L = 20^2 + 14^2</math>  <math>L = \sqrt{20^2 + 14^2}</math>  <math>= 24.41\text{cm}</math>  <math>146.5 - 24.41</math>  <math>= 122.09\text{cm}</math></p> <p>c.) Curved surface  Arc of the frustum  <math>\pi \times 84 \times 146.5 - \pi \times 14 \times 24.41</math>  <math>37,601.96</math></p> <p>Curved surface of the cylinder  <math>2\pi \times \frac{22}{7} \times 14 \times 40 = 3520\text{cm}^2</math>  Base <math>\pi \times 14^2 = 616\text{cm}^2</math>  Top <math>\pi \times 84^2 = 22,176\text{cm}^2</math>  Total surface area  <math>37601.96 + 3520 + 616 + 22176 =</math>  <math>63,913.96\text{cm}^3</math></p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>10</p>	<p>Follow through</p> <p>Area of the top and base</p>
20.	<p>a) <math>\angle AOD = 76^\circ</math>  Angle subtended at the centre by an arc is twice the angle subtended on the circumference by the same arc.</p> <p>b.) <math>\angle BDC = 28^\circ</math>  angle subtended by the same arc on the circumference i.e. arc BC</p> <p>c.) <math>\angle ACB = 62^\circ</math>  angle subtended by a diameter on the circumference is equal to <math>90^\circ</math></p> <p>d.) <math>\angle FDC = 52^\circ</math>  Alternate segment theorem</p> <p>e.) <math>\angle ATD = 42^\circ</math>  Sum angles of a quadrilateral</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>10</p>	<p><math>\checkmark</math> reason</p> <p><math>\checkmark</math> reason</p> <p><math>\checkmark</math> reason</p>
21.	<p>a.)</p> <p>i.) <math>\vec{PQ} = \vec{PO} + \vec{OQ}</math>  <math>-\mathbf{p} + \mathbf{q}</math>  <math>\mathbf{p} - \mathbf{q} + \frac{1}{3}\mathbf{q}</math>  <math>\mathbf{p} - \frac{2}{3}\mathbf{q}</math></p>	<p>B1</p> <p>M1</p> <p>A1</p>	

	<p>b.)</p> <p>i.) <math>\vec{ST} = \vec{SO} + \vec{OT}</math>  <math>-\frac{4}{3}\mathbf{q} + \mathbf{p} + m\mathbf{p}</math></p> <p>ii.) <math>\vec{ST} = n(\mathbf{p} - \frac{2}{3}\mathbf{q})</math>  <math>n\mathbf{p} - \frac{2}{3}n\mathbf{q} = -\frac{4}{3}\mathbf{q} + \mathbf{p}(1+m)</math>  <math>n=1+m</math>  <math>-\frac{2}{3}n = -\frac{4}{3}</math>  <math>n=2</math>  <math>m=1</math></p> <p>iii.) <math>RS = \frac{2}{3}\mathbf{q} + \mathbf{p}</math>  <math>ST = 2(-\frac{2}{3}\mathbf{q} + \mathbf{p})</math></p> <p><math>\therefore \vec{ST} = 2\vec{RS}</math>  S is common  ST // RS  R, S and T are collinear</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>10</p>	<p>For equating the two vectors</p> <p>For extracting the coefficients</p> <p>For n=2 and m=1</p>
22.	<p>a.) X 0 0.5 1 1.5 2 2.5  Y 3 3.25 4 5.25 7 9.25</p> <p>X 3 3.5 4 4.5 5  Y 12 15.25 19 23.25 28</p> <p>X 5.5 6  Y 33.25 39</p> <p>b.) X 0.5 1.5 2.5 3.5 4.5  Y 3.25 5.25 9.25 15.25 23.25</p> <p>X 5.5  Y 33.25</p> <p>Area = <math>\frac{1}{2}(3.25 + 5.25 + 9.25 + 15.25 + 23.25 + 33.25)</math>  89.5 sq. Units</p> <p>c.) <math>\int_0^6 (x^2 + 3) dx</math>  <math>\left[ \frac{x^3}{3} + 3x \right]_0^6</math>  <math>\frac{6^3}{3} + 3 \times 6 - 0</math>  72+18  90</p>	<p>B2</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>For all 9 <math>\sqrt{\quad}</math> values filled .award B1 for at least 6 correctly filled values.</p> <p>For mid-ordinates 3.25, 5.25, 9.25, 15.25, 23.25 and 33.25</p> <p>For <math>\int</math> integration</p> <p>For substitution of limits</p>

	d.) $\frac{0.5}{90} \times 100$ $\frac{5}{9}\%$	M1 A1	Accept 0.55.....or 0.5556																
23.	a.) $y+2 = bx^n$ $\log(y+2) = \log b + n \log x$ b.) <table style="display: inline-table; border: none;"> <tr> <td><math>\log x</math></td> <td>0</td> <td>0.1761</td> <td>0.3010</td> </tr> <tr> <td><math>\log(y+2)</math></td> <td>0.6990</td> <td>1.2274</td> <td>1.6021</td> </tr> <tr> <td><math>\log x</math></td> <td>0.3979</td> <td>0.4771</td> <td>0.5441</td> </tr> <tr> <td><math>\log(y+2)</math></td> <td>1.8928</td> <td>2.1303</td> <td>2.3312</td> </tr> </table>  $\log x$ 0.6021 $\log(y+2)$ 2.5051  (0.0.7) (0.3,1.6)  $n = \frac{1.6 - 0.7}{0.3}$ $n = 3$  $\log b = 0.7$ $b = 5.012$ $y = -2 + 5.012x^3$	$\log x$	0	0.1761	0.3010	$\log(y+2)$	0.6990	1.2274	1.6021	$\log x$	0.3979	0.4771	0.5441	$\log(y+2)$	1.8928	2.1303	2.3312	B1 B2  S1 P1 L1  M1 A1  B1 B1 10	Values of For $\log x$ and $\log$ ( $y+2$ )  Linear scale Plotting Line of best fit drawn
$\log x$	0	0.1761	0.3010																
$\log(y+2)$	0.6990	1.2274	1.6021																
$\log x$	0.3979	0.4771	0.5441																
$\log(y+2)$	1.8928	2.1303	2.3312																
24.																			

