

NAME..... INDEX NO. ....

**121/1**  
**MATHEMATICS PAPER 1**  
**AUGUST 2021**  
**2 ½ HRS**  
**FORM 4 MARKING SCHEME**

**CASPA AMUKURA PARISH EXAM**  
**Kenya Certificate of Secondary education**  
**MATHEMATICS PAPER 1**  
**MARKING SCHEME**

**INSTRUCTIONS TO CANDIDATES**

1. *Write your name, Admission number and class in the spaces provided.*
2. *Sign and write date of the examination in the spaces provided.*
3. *The paper contains TWO sections: Section A and B*
4. *Answer ALL questions in section I and **STRICTLY ANY FIVE** questions from section II.*
5. *All working and answers must be written on the question paper in the spaces provided below each question.*
6. *Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.*
7. *Marks may be awarded for correct working even if the answer is wrong.*
8. *Non-programmable silent electronic calculators and KNEC Mathematical tables may be used except where stated otherwise.*

**FOR EXAMINERS USE ONLY**

**SECTION A**

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	TOTAL

**SECTION B**

17	18	19	20	21	22	23	24	25	26	27	TOTAL

SECTION I - 50 MARKS

$$1) \left(\frac{19}{5} - \frac{5}{8}\right) + \frac{2}{3} \text{ of } \frac{6}{5}$$

$$= \frac{80 - 35}{56} + \frac{4}{5}$$

$$= \frac{45}{56} + \frac{4}{5}$$

$$= \frac{225 + 224}{280}$$

$$= \frac{449}{280} \checkmark$$

$$\frac{3}{4} + \frac{13}{7} \div \frac{4}{7} \text{ of } \frac{3}{5}$$

$$= \frac{3}{4} + \frac{13}{7} \times \frac{7}{4} \text{ of } \frac{3}{5}$$

$$= \frac{3}{4} + \frac{13 \times 3}{4}$$

$$= \frac{21 + 36}{28}$$

$$= \frac{57}{28} \checkmark$$

$$\frac{449}{280} \times \frac{28}{57} = \frac{449}{570} \checkmark$$

Total

2

$$2a + 5b = 16$$

$$3a + 7b = 16$$

$$6a + 15b = 48$$

$$6a + 14b = 32$$

$$b = 16 \checkmark$$

$$a = -32 \checkmark$$

TOTAL = 03

3

$$2 - x - x^2 = 2 - 2x + x - x^2$$

$$= 2(1-x) + x(1-x)$$

$$= (2+x)(1-x) \checkmark$$

$$3x^2 - 3x + 1 = 1$$

$$= 3x(x-1) + 1(x-1)$$

$$= (3x+1)(x-1) \checkmark$$

$$\therefore = \frac{(2+x)(1-x)}{(3x+1)(x-1)}$$

$$= -\frac{2+x}{3x+1} \checkmark$$

Total = 03

4

$$2x + x - 30 = 90 \checkmark$$

$$3x = 120$$

$$x = 40 \checkmark$$

Total = 02

5

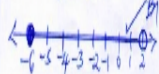
$$3x - 4 = 3x + 2$$

$$-6 = x \checkmark$$

$$3x + 2 = 10 - x$$

$$4x = 8$$

$$x = 2 \checkmark$$



TOTAL = 03

6

$$LSF = \frac{18}{24} = \frac{3}{4} \checkmark$$

$$VSF = \left(\frac{3}{4}\right)^3 = \frac{27}{64} \checkmark$$

$$\frac{27}{64} = \frac{x}{320} \checkmark$$

$$x = 135 \text{ cm}^3 \checkmark$$

TOTAL = 04

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$2^{3(2x-2)} \times 2^{4(2)} = 4^7$ $2^{3(2x-2)} \times 2^{4(2)} = 2^{-2}$ $9x - 6 + 2x = -2$ $11x = 4$ $x = \frac{4}{11}$ <p>Total 02</p>	<p>⑩ Let ext angle = x.</p> $3\frac{1}{2}x + x = 180$ $4.5x = 180$ $x = 40$ <p>Total 02</p>
$P \propto \frac{Q}{\sqrt{R}}$ $P = k \frac{Q}{\sqrt{R}}$ $\text{New } P = \frac{H}{\sqrt{10.81}} P$ $= \frac{1.1}{0.9} P = 1.2222P$ <p>% Increase = <math>0.2222 \times 100</math></p> $= 22.22\%$ <p>Total 03</p>	<p>⑪ <math>AC = B</math></p> $C = A^{-1}B$ $= \frac{1}{5} \begin{pmatrix} 4 & -2 \\ 1 & 2 \end{pmatrix} \begin{pmatrix} -1 & 3 \\ 2 & -1 \end{pmatrix}$ $= \frac{1}{5} \begin{pmatrix} -10 & 15 \\ 5 & -5 \end{pmatrix} = \begin{pmatrix} -2 & 3 \\ 1 & -1 \end{pmatrix}$ <p>Total 03</p>
<p>⑫</p> $2x + 5y = 275$ $4x + 7y = 415$ $8x + 20y = 1100$ $8x + 14y = 830$ $6y = 270$ $y = 45$ $x = 25$ <p>Total 04</p>	<p>⑬ W : S : D</p> $4 : 3 : 2$ <p>Let total amount = x</p> $\left(\frac{4}{9} - \frac{2}{9}\right)x = \text{sh } 120,000$ $\frac{2}{9}x = 120,000$ $x = \text{sh } 540,000$ <p>Total 02</p>
<p>⑭ Sales = <math>\frac{100-2}{100} \times \text{sh } 240,000</math></p> $= \frac{98}{100} \times \text{sh } 240,000$ $= \text{sh } 233,200$ <p>% Commission = <math>\frac{1660}{333200} \times 100</math></p> $= 5\%$ <p>Total 03</p>	

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$$\begin{aligned}
 14 \quad 0.3758 &= \frac{1}{0.3758} \\
 &= \frac{1}{1 \times 3.758 \times 10^{-1}} \\
 &= 1 \times 0.2661 \times 10^1 \\
 &= 2.661 \quad \checkmark \\
 \sqrt{0.125} &= 0.5 \quad \checkmark \\
 \therefore &= 2.661 \times 0.5 \quad \checkmark \\
 &= 1.3305 \\
 &= 1.331 \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 \text{Dollars} &= \frac{3348880}{74.59} \\
 &= 44951 \text{ dollars} \\
 \text{TOTAL} &= 03.
 \end{aligned}$$

$$\begin{aligned}
 15 \quad \text{Area} &= \frac{150}{360} \times \frac{22}{7} \times 7 \times 7 \quad \checkmark \\
 &= 64.17 \text{ cm}^2 \\
 \therefore 64.17 &= \frac{22}{7} \times R \times 7 \quad \checkmark \\
 2.917 &= R \\
 2.9 &= R \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 16 \quad \text{Amount on arrival} &= 24000 \times 147.87 \\
 &= 3,548,880 \quad \checkmark \\
 \text{Balance} &= \text{sh } 3,548,880 - \text{sh } 200,000 \\
 &= \text{sh } 3,348,880 \quad \checkmark
 \end{aligned}$$

SECTION II - 50 MARKS

$y - 4x = 5$  ----- (2)  
 $4y - 9x = 13$  ----- (1)

$4y - 16x = 20$  ✓ M1  
 $4y - 9x = 13$   
 $-7x = 7$   
 $x = -1$  ✓ A1  
 $y = 1$   
 Hence P(-1, 1) ✓ B1

$X = 2(5) - (-1) = 11$  ✓  
 $Y = 2(3) - 1 = 5$  ✓  
 Hence R(11, 5) ✓ B1

SP of RQ  
 Hence  $M_1 = M_2 = 4$   
 $\therefore 4 = \frac{y-11}{x-5}$  ✓ M1  
 $y - 11 = 4(x - 5)$   
 $y = 4x - 20 + 11$   
 $y = 4x - 9$  ✓ A1

(d) PR  $\therefore P(-1, 1)$  and  $(5, 3)$   
 Grad =  $M_1 = \frac{3-1}{5-(-1)} = \frac{2}{6} = \frac{1}{3}$   
 $M_2 = -3$  ✓ A1  
 Hence  $-3 = \frac{y-3}{x-5}$  ✓ M1  
 $y - 3 = -3(x - 5)$   
 $y = -3x + 15 + 3$   
 $y = -3x + 18$  ✓ A1

TOTAL 10 MARKS

18)  $\overrightarrow{MS}$  →  $\overrightarrow{NS}$

Speed = 80 km/h  
Dist = 80 km/h

19)  $\overrightarrow{CS}$   
Component  
will be 1/2

a) Distance = 80 x 4 hr  
Covered = 4 km / hr

b) Relative distance = 510 - (80 x 4 + 100 x 1) / M1  
= 510 - (320 + 100)  
= 510 - 420  
= 90 km / hr

Time taken =  $\frac{270 \text{ km}}{120 \text{ km/h}} = 2.25 \text{ hr}$   
 $\frac{150}{120} = 1.25 \text{ hr}$

Time of day = 6:00 am + 1 hr + 1 hr + 1 hr + 1 hr  
= 6:00 am + 3 hr 15 mins  
= 9:15 am / M1

c) Distance from NRB =  $100 \times 1 + 100 \times \frac{1}{2}$   
= 100 + 50  
= 150 km / hr

d) Time taken =  $\frac{510 \text{ km}}{80 \text{ km/h}} = 6.375 \text{ hr}$   
= 6 hr 23 mins

Time of day = 6:00 am + 6 hr 23 mins  
= 12:23 pm / B1

TOTAL 10 MARKS

b)  $\tan 42 = \frac{h}{h \cos 42}$   
 $h = \frac{h}{\cos 42}$   
 $h = \frac{h}{\cos 42}$   
 $\tan 42 = 0.9004$   
 $0.9004 = 0.5774(t+1)$   
 $0.9004 = 0.5774t + 0.5774$   
 $0.9004 - 0.5774 = 0.5774t$   
 $0.323 = 0.5774t$   
 $t = \frac{0.323}{0.5774}$   
 $t = 0.558 \text{ hr}$   
 $= 5.36 \text{ hr}$   
 $= 5:40 \text{ M1}$

c)  $\tan 30 = \frac{8.362}{4.530} \sqrt{M1}$   
 $4.530 = 8.362 \tan 30$   
 $= 4.828 = 4.8 \text{ M1}$

d)  $\tan 30 = \frac{8.362}{4.530} \sqrt{M1}$   
 $4.530 = 8.362 \tan 30$   
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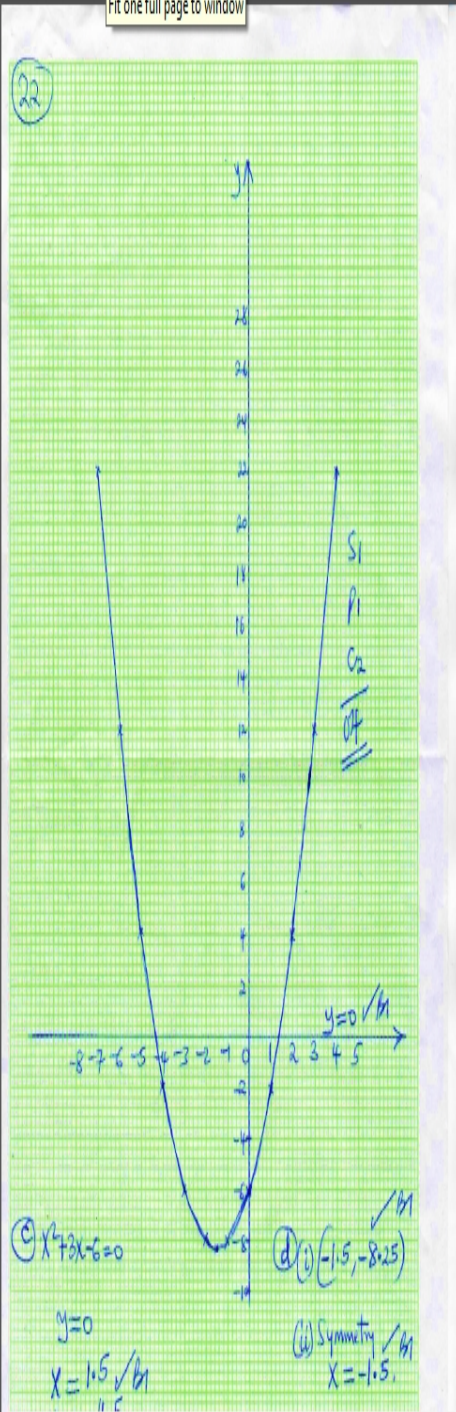
e)  $\tan 30 = \frac{8.362}{4.530} \sqrt{M1}$   
 $4.530 = 8.362 \tan 30$   
 $= 4.828 = 4.8 \text{ M1}$

f)  $\tan 30 = \frac{8.362}{4.530} \sqrt{M1}$   
 $4.530 = 8.362 \tan 30$   
 $= 4.828 = 4.8 \text{ M1}$

TOTAL 10 MARKS



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<p>23) Area of <math>= \sqrt{s(s-a)(s-b)(s-c)}</math>                  (a) <math>\Delta ABC = \sqrt{14 \times 3 \times 4 \times 7}</math>  <math>= \sqrt{1156}</math>  <math>= 34.292</math>  <math>A = \frac{1}{2} ab \sin C</math>  <math>34.292 = \frac{1}{2} \times 11 \times 10 \sin A \sqrt{M_1}</math>  <math>\sin A = \frac{34.292 \times 2}{110}</math>  <math>= 0.6235 \checkmark M_1</math>  <math>A = \sin^{-1} 0.6235</math>  <math>= 38.57</math>  <math>= 38.6^\circ \checkmark A_1</math></p> <p>(b) Radius <math>= \frac{a}{2 \sin A}</math>  <math>= \frac{7}{2 \sin 38.57} \checkmark M_1</math>  <math>= 5.614</math>  <math>= 5.6 \checkmark A_1</math></p> <p>(c) Shaded Area <math>= \pi r^2 - \frac{1}{2} ab \sin C</math>  <math>= \frac{22}{7} \times 5.6^2 - 34.292 \checkmark M_1</math>  <math>= 99.05 - 34.292 \checkmark M_1</math>  <math>= 64.758</math>  <math>= 64.8 \checkmark A_1</math></p> <p style="text-align: center;"><u>TOTAL 10 MARKS</u></p>	<p>Alternative Approach</p> <p><math>\cos A = \frac{11^2 + 10^2 - 7^2}{2 \times 11 \times 10}</math>  <math>= \frac{172}{220} = 0.7818 \checkmark</math>  <math>A = \cos^{-1}(0.7818)</math>  <math>= 38.57</math>  <math>= 38.6 \checkmark</math></p> <p>Area of Circle and                  Evidence of Subtraction</p>
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$\sin X = \frac{2}{36} = 0.05556$   
 $X = \sin^{-1}\left(\frac{2}{36}\right)$   
 $= 3.185^\circ$   
 $\angle AOE = 90 + 3.185$   
 $= 93.185 = 93.2^\circ \checkmark$   
 $\angle AOE = 360 - 2 \times 93.185$   
 $= 360 - 186.37$   
 $= 173.63 = 173.6^\circ \checkmark$   
 $\text{Arc length} = \frac{\theta}{360} \times 2\pi r$   
 $= \frac{173.63}{360} \times 2 \times \frac{22}{7} \times 36$   
 $= 15.16 = 15.2 \checkmark$   
 $\text{Arc length} = \frac{186.37}{360} \times 2 \times \frac{22}{7} \times 36$   
 $= 22.78 = 22.8 \checkmark$   
 $AB = \sqrt{36^2 - 2^2}$   
 $= \sqrt{1292}$   
 $= 35.94 = 35.9 \checkmark$   
 $\text{Total length} = 15.16 + 22.78 + 2 \times 35.94$   
 $= 109.82 \checkmark$

M	Ratio
A	Angle X = 3.185
B	Angle AOE
B	Obtuse angle AOE
B	Arc AFE
B	Reflex angle BEO
B	Arc BEO
B	Tangential length
M	Addition
A	CAD

TOTAL MARKS 10