

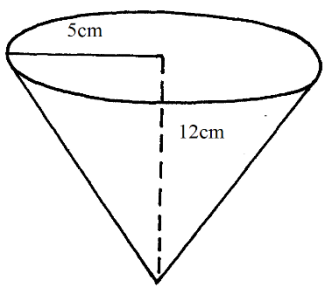


MARKING SCHEME
THE ROYAL EXAM SERIES

Kenya Certificate of Secondary Education



MATHEMATICS 121/1

Qn	working	Marks	REMARKS
1.	$\frac{1.9 \times 0.032 \times 10000}{20 \times 0.0038 \times 10000}$ $= \frac{19 \times 32}{20 \times 38}$ $= \frac{16}{20}$ $= \frac{8}{10}$	M1 B1 A1	
		03	
2.	$5 \times \frac{1}{8.29 \times 10^{-2}} - 14 \times \frac{1}{5.81 \times 10^{-1}}$ $5 \times 0.1206 \times 10^2 - 14 \times 0.1721 \times 10$ $= 60.3 - 24.094$ $= 36.206$	M1 M1 A1	
		03	
3.	$\cos = \frac{Ads}{hps} = \frac{8}{10}$ <p>QR=8 and PQ=10 $PR^2 = PQ^2 - QR^2 = 10^2 - 8^2$ $PR = \sqrt{36} = 6$</p> <p>(a) $\sin \theta = \frac{6}{10}$ or $\frac{3}{5}$ (b) $\tan (90 - \theta) = \frac{QR}{PR} = \frac{8}{6}$ or $\frac{4}{3}$</p>	B1 M1 A1	
		03	
4.	 <p>SA = $\pi r l$ $l = \sqrt{5^2 + 12^2}$</p>	M1 M1 A1	

	$=50\text{km}$ $(ii) \sin \theta = \frac{40}{50} = 0.8$ $\theta = 53.13$ $\approx 53^{\circ}$	A1	
		03	
10.	$L_1 = x \geq 0$ $L_2 = \frac{x}{5} + \frac{y}{4} = 1$ $4x + 5y = 20$ $4x + 5y \leq 20$ $L_3: \frac{x}{4} + \frac{y}{-3} = 1$ $3x - 4y = 12$ $\therefore 3x - 4y < 12$	B1 B1 B1 A1	
		04	
11.	Let ext. $< x^{\circ}$ Interior $\leq 3x + 20^{\circ}$ $x + 3x + 20^{\circ} = 180^{\circ}$ $4x = 160^{\circ}$ $4x = 160^{\circ}$ $x = 40$ $\frac{360}{40} = 9$ sides	M1 M1 A1	
		03	
12	$s = \sqrt{s(s-a)(s-b)(s-c)}$ $s = \frac{1}{2}(4.8 + 6.8 + 5.7) = 8.4$ $Area = \sqrt{8.4(2.7)(3.6)(2.1)}$ $= 18.05 - 13.0943$ $= \sqrt{171.4608} = 13.0943$ $= 4.9557$ ≈ 4.96	BI M1 A1	
		03	
13.	Change to base 3 $3^{2(x-1)} \times 3^{2x+1} = 3^5$ $2(x-1) + 2x + 1 = 5$ $2x - 2 + 2x + 1 = 5$ $4x - 1 = 5$ $4x = 6$ $x = 1.5$	M1 M1 A1	

										03																
14.	<table border="1"> <tr> <td>Mean in kg</td> <td>41-50</td> <td>51-55</td> <td>56-65</td> <td>66-70</td> <td>71-80</td> </tr> <tr> <td>Frequency</td> <td>20</td> <td>70</td> <td>50</td> <td>50</td> <td>10</td> </tr> </table> <p>b) Modal frequency is 70.</p>									Mean in kg	41-50	51-55	56-65	66-70	71-80	Frequency	20	70	50	50	10	B1			B1	B1
Mean in kg	41-50	51-55	56-65	66-70	71-80																					
Frequency	20	70	50	50	10																					
										03																
15.	<p>L.S.F=V.S.F</p> $lsf = \sqrt[3]{\frac{4752}{1408}}$ $= 1.5$ <p>l.s.f²=A.S.F</p> $1.5^2 = \frac{\text{Area of larger cylinder}}{352}$ <p>Area of larger cylinder 792cm²</p>									M1			A1													
										02																
16.	<p>Reduce $5y+2x=7$ in the form $y=mx+c$</p> $\therefore y = \frac{-2}{5}x + \frac{7}{5}$ <p>But gradient $= \frac{k-5}{3-2} = \frac{k-5}{5}$</p> $= \frac{k-5}{5} = \frac{2}{3}$ <p>K=3</p>																									
17	<p>(a) $\frac{5 \times 25 + 2 \times 30 + 45 \times 1}{8} = 28.75$</p> <p>Profit $28.75 \times \frac{20}{100} = sh.5.75$</p> <p>(b) (i) $New Price = \frac{28.75}{100} \times 110 \times \frac{115}{100} = 36.40$</p> <p>(ii) $\frac{28.75 \times 110}{100} = 31.60$</p> <p>New Profit $\frac{45 - 31.60}{31.60} \times 100$</p> $= \frac{13.4}{31.60} \times 100$ $= 42.41\%$																									
18	X	-3	-2	-1	0	1	2	3	4																	

X^2	9	4	1	0	1	4	9	16
$2x^2$	18	8	2	0	2	8	18	32
$-3x$	9	6	3	0	-3	-6	-9	-12
-5	-5	-5	-5	-5	-5	-5	-5	-5

Y	22	9	0	-5	-6	-3	4	15
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Mini

mum at point (1,6)

$$y = 2x^2 - 5x - 5$$

$$0 = 2x^2 - 3x - 5$$

$$Y=0$$

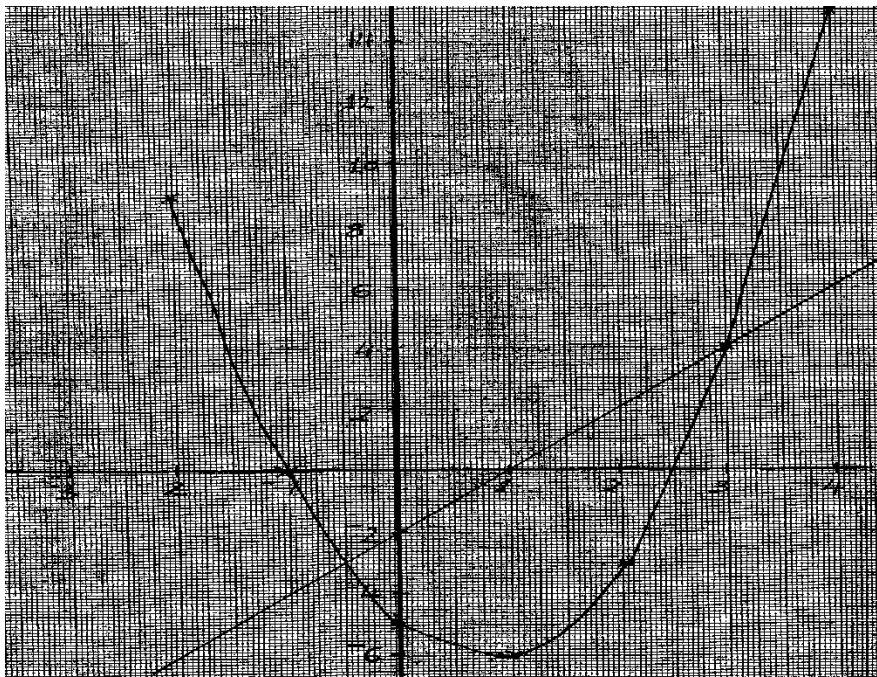
$$X=-1 \text{ or } x = 2.5$$

$$y = 2x^2 - 3x - 5$$

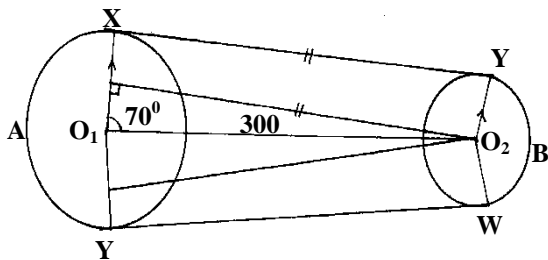
$$0 = 2x^2 - 5x - 3$$

$$Y = 2x - 2$$

$$X = -0.5 \text{ or } x = 3$$



19



	<p>a) $XV = MO_2 = 300 \sin 70 = 281.9 \text{cm}$</p> <p>b) $YBW = \frac{140}{360} \times 2\pi r$</p> <p>$MO_1 = 300 \cos 70 = 102.6 \text{cm}$</p> <p>Radius of small circle = $180 - 102.6 = 77.4 \text{cm}$</p> <p>$VBW = \frac{140}{360} \times 2 \times 3.142 \times 77.4 = 189.1 \text{cm}$</p> <p>c) $XAY = \frac{220}{360} \times 2\pi \times 180$</p> <p>$= \frac{220}{360} \times 2 \times 3.142 \times 180 = 691.2 \text{cm}$</p> <p>d) Length of conveyor belt</p> <p>$= 281.9 \times 2 + 189.1 + 691.2$</p> <p>$= 1444.1 \text{cm}^2$</p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	
20	<p>$11.45 = 1 \frac{1}{2} \text{h}$</p> <p>Distance moved by bus = $1.5 \times 60 = 90 \text{km}$</p> <p>Distance btwn 2 vehicles</p> <p>$540 - 90 = 450$</p> <p>R.speed = $60 + 90 = 150 \text{km/h}$</p> <p>T.taken to meet = $450 \div 150 = 3 \text{h}$</p> <p>$= 1.15 + 3 = 4.15 \text{p.m}$</p> <p>b) Total time moved by bus when they met.</p> <p>$16.15 - 11.45 = 4 \frac{1}{2} \text{hrs}$</p> <p>Distance from A = 4.5×60</p> <p>$= 270 \text{km}$</p> <p>c) time taken by matatu to travel from B to A = $540 \div 90 = 6 \text{hrs}$</p> <p>$\therefore$ Time matatu reaches A</p> <p>$13.15 + 6 = 19.15 \text{hrs}$</p> <p>$\therefore$ Time traveled by bus until matatu reaches A</p> <p>$= 19.15 - 11.45 = 7 \frac{1}{2} \text{hrs}$</p> <p>Distance moved by bus from A = 7.5×60</p> <p>Hence outside town B</p> <p>$= 540 - 450$</p> <p>$= 90 \text{km}$</p>		
21	<p>$\frac{y + 2}{x - 8} = \frac{-4 + 2}{4 - 8} = \frac{1}{2}$</p> <p>$2y + 4 = x - 8$</p> <p>$\Rightarrow x - 2y - 12 = 0$</p> <p>a) $\therefore u = 1, b = -2 \text{ and } c = -12$</p>		

	$y = \frac{x}{2} - 6, \text{ when } y = 0$ $\frac{x}{2} - 6 = 0 \Rightarrow x = 12$ <p>\therefore Coordinate s of pane (12,0)</p> <p>(b)</p> $\frac{y}{x - 12} = -2$ $\Rightarrow y = 24 - 2x$ <p>but when $x = 0, y = 24$</p> <p>(c) \therefore Coordinate s of Q are (0, 24)</p> $QP = \sqrt{(12 - 0)^2 + (0 - 24)^2}$ <p>(d) $= \sqrt{144 + 576} = 26.83 \text{ Units}$</p>		
22	<p>(a) volume of solid = volume of cone + volume of hemisphere</p> $= \frac{1}{3}\pi r^2 h + \frac{1}{2} \times \frac{4}{3} \pi r^3 = 36$ $= \frac{1}{3}\pi r^2 + \frac{2}{3}\pi r^3 = 36$ $= \frac{4}{3}\pi r^3 = 36$ $\frac{4}{3}\pi r^3 = 36$ $r^3 = \frac{36 \times 3}{4 \times 3.142}$ $r^3 = 8.593$ $r = 2.048\text{cm}$ <p>(b) Let the level rise be x</p> $\pi r^2 x = 36$ $x = \frac{36}{3.142 \times 81}$ $= \frac{36}{254.502}$ $= 0.14\text{cm}$ <p>(c) volume = $\frac{1}{2} Ah$</p> $= \frac{1}{3} x A \times 4.2 = 36$ $A = \frac{36 \times 3}{4.2}$ $= 25.71\text{cm}^2$ <p>(d) Density = $\frac{\text{mass}}{\text{volume}}$</p> $= \frac{14.4}{36} \times 1000\text{Kg/m}^3$ $= 400\text{Kg/m}^3$		
23	<p>a) i) $\overline{AB} = \underline{b} \quad \underline{a}$</p> <p>ii) $BQ = \overline{BO} = \overline{OQ} = \frac{1}{2} \underline{a} - \underline{b}$</p>		

$$\overrightarrow{BX} = h\left(\frac{1}{2}\underline{a} - \underline{b}\right)$$

$$\overrightarrow{OX} = \underline{b} + h\left(\frac{1}{2}\underline{a} - \underline{b}\right)$$

$$\frac{1}{2}h\underline{a} + (1-h)\underline{b}$$

(c)

$$\overrightarrow{OX} = R \overrightarrow{OP}$$

$$\text{but } \overrightarrow{OP} = \frac{1}{4}\underline{a} + \frac{3}{4}\underline{b} = \frac{1}{4}(\underline{a} + 3\underline{b})$$

$$OX = \frac{R}{4}(\underline{a} + 3\underline{b})$$

$$OX = OX_2$$

$$\frac{1}{2}h\underline{a} + (1-h)\underline{b} = \frac{1}{4}R\underline{a} = \frac{3}{4}k\underline{b}$$

$$\frac{1}{2}h = \frac{1}{4} \Rightarrow (2h - k = 0)$$

$$1 - h = \frac{3}{4} \Rightarrow (-4 - 3h = -4)$$

$$4h - 2k = 0$$

$$4h - 3k = -4$$

$$-5k = -4$$

$$k = \frac{4}{5}$$

$$h = \frac{2}{5}$$

24

Length (cm)	Mid pt (x)	F	xf	CF
118 - 126	122	3	366	3
127 - 135	131	4	524	7
136 - 144	140	10	1400	17
145 - 153	149	12	1788	29
154 - 162	158	5	790	34
163 - 171	167	4	668	38
172 - 180	176	2	352	40
		40	5888	

(a) (i) Modal class \Rightarrow 145 - 153

(ii) Median class 145 - 153

(b) (i) Mean of feeding

$$x = \frac{\sum xf}{\sum f}$$

$$= \frac{5888}{40}$$

$$147.2$$

$$(ii) \text{ Median} = L \left(\frac{\frac{n+1}{2} - c}{f} \right) i$$

$$= 144.5 + \left(\frac{41 - 17}{2} \right) 9$$

$$144.5 + \frac{20.5 - 17}{2} \times 9$$

$$144.5 + 2.625$$

B1
B1

B1
B1

B1
B1

B1
B1

B1
B1

	= 147.125		
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