****

**JARAMOGI OGINGA ODINGA UNIVERSITY OF SCIENCE AND TECHNOLOGY SCHOOL OF BIOLOGICAL AND PHYSICAL SCIENCES**

**UNIVERSITY EXAMINATION FOR THEDEGREE OF BACHELOR OF EDUCATION (SCIENCE)**

**4TH YEAR 2ND SEMESTER**

**MAIN**

**REGULAR**

**COURSE CODE: SPH 402**

**COURSE TITLE: STATISTICAL MECHANICS**

**EXAM VENUE: STREAM: (BED SCI)**

**DATE: 18/4/2017 EXAM SESSION:**

**TIME: 2:00HRS**

**\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**Instructions:**

1. **Answer question 1 (Compulsory) and ANY other 2 questions.**
2. **Candidates are advised not to write on the question paper.**
3. **Candidates must hand in their answer booklets to the invigilator while in the examination room.**

**Useful constants**







***QUESTION 1 (30 MARKS)***

(a) Define the following terms.

(i) Statistical Physics  **(1 mark)**

(ii) Canonical ensemble **(1 mark)**

(iii) Grand canonical ensemble  **(1 mark)**

(iv) Phase space  **(1 mark)**

(b) The Hamiltonian of a given system in phase space is given by 

Determine the Hamiltonian canonical equations of motion. **(3 marks)**

(c) Two bosons are in an energy level with degeneracy of . Determine the number

of microstates of these bosons.  **(3 marks)**

(d) State **TWO**features of particles obeying Maxwell-Boltzmann statistics.

**(2 marks)**

(e) By using Helmholtz free energy, derive expressions for entropy, pressure and

chemical potential. **(4 marks)**

(f) Derive the equation for the partition function of a spin- paramagnetic system.

**(3 marks)**

(g) Explain the formation of Bose-Einstein condensate. **(2 marks)**

(h) Show that the average internal energy in a canonical ensemble is given by

 where each symbol has its usual meaning.**(3 marks)**

(i) Explain the term black body as used in Statistical Physics  **(2 marks)**

(j) Determine the percentage error in the use of Stirling’s formula to calculate 

for a system of  particles.  **(4 marks)**

***Attempt any TWO questions in this section***

***QUESTION 2 (20 MARKS)***

(a) Show that the Maxwell-Boltzmann distribution function is given by

**(12 marks)**

(b) Blackbody radiation in a box of volume and at temperature  has internal

energy and pressure , where is the Stefan-Boltzmann

constant. Determine the entropy and chemical potential in terms of .

**(8 marks)**

***QUESTION 3 (20 MARKS)***

(a) Consider a system of particles that obey Fermi-Dirac statistics with a

a degeneracy of in each energy level. Given that the energy levels are equally

spaced and the total energy per macrostate is where ,  and so

on,determine the statistical weight of the system. **(10 marks)**

(b) Obtain an expression for the entropy of a thermodynamic system in terms of

the statistical weight. **(10 marks)**

***QUESTION 4 (20 MARKS)***

(a) Show that the energy density in blackbody radiation is given by

**(15 marks)**



(b) Show that the maximum value of the wavelength for which  obtained in

4 (a) is maximum is obtained from **(5 marks)**

***QUESTION 5 (20 MARKS)***

(a) Derive the average internal energy of a system of -independent particles

in the form **(7 marks)**

(b) Determine the conditions under which a composite isolated system C resulting

interaction of two isolated systems A and B attains thermodynamic equilibrium.

**(13 marks)**