

2. Angle properties of circles

1.	$\angle QRO = 30^\circ$ Base angles of isosc. Triangle $\angle ROT = 100 - 120 = 60^\circ$ \angle s on straight line $\angle ROT = 60^\circ$ $\angle ORP = 60^\circ$ Base angles of Isoc triangle $\angle QRS = 90^\circ$ diameter subtended right angle at the circumference (a) $\angle SRQ = 90^\circ - 30 - 30^\circ$ $\quad\quad\quad = 30^\circ$ $\angle QRO + ORP + SRP = 90^\circ$ Diam. Subt 90° at circumference (b) $ORP = 60^\circ$ Base angle of isosceles triangle (c) OP to MPT $\angle OPT = 90^\circ$ Radius meets tangent at 90° $\angle RTP = 90^\circ - \angle OPR$ $\quad\quad\quad = 90^\circ - 30^\circ$ $\quad\quad\quad = 60^\circ$ (d) $\angle STP = 180^\circ - \angle OPT 90^\circ - \angle POT 60^\circ$ $\quad\quad\quad$ Angle sum of triangle $\quad\quad\quad = 30^\circ$ (e) $\angle QPM = \angle QRP = 60^\circ$ Angles in alternate segment	B1 B1 B1 B1 B1 B1 B1 B1 B1 B1	
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1. Area of $\triangle AXY = \frac{1}{2} \times 4^2 \times \sin 97.2^\circ$
 $\quad\quad\quad = 7.94 \text{ cm}^2$
 Area of sector $AXY = \frac{97.2}{360} \times \pi \times 4^2$

$$= 13.57 \text{ cm}^2$$

$$\text{Area of shaded part} = 13.57 - 7.94 = 5.63 \text{ cm}^2$$

$$\begin{aligned} \text{Area of } \triangle BXY &= \frac{1}{2} \times 6^2 \sin 30 \\ &= 9 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of sector BXY} &= \frac{30}{360} \times \pi \times 6^2 \\ &= 9.42 \text{ cm}^2 \end{aligned}$$

Area of shaded part

$$= (9.42 - 9) \text{ cm}^2 = 0.42 \text{ cm}^2$$

$$\text{Area of shaded region} = (5.63 + 0.42) \text{ cm}^2 = 6.05 \text{ cm}^2$$

$$\begin{aligned} 2. \text{ (i) } \angle AOB &= 2 \angle ACB \\ &= 100^\circ \end{aligned}$$

$$\begin{aligned} \angle OAB &= \frac{180 - 100}{2} \text{ Base angles of Isosceles } \triangle \\ &= 40^\circ \end{aligned}$$

$$\begin{aligned} \text{(ii) } \angle ADC &= 180^\circ - 70^\circ \\ &= 110^\circ \end{aligned}$$

$$\begin{aligned} 3. \quad \frac{2}{5} \div \frac{1}{2} \text{ of } \frac{4}{9} - 1\frac{1}{10} \\ &= \frac{2}{5} \div \frac{1}{2} \times \frac{4}{9} - 1\frac{1}{10} \\ &= \frac{2}{5} \times \frac{9}{2} - 1\frac{1}{10} \\ &= \frac{9}{5} - 1\frac{1}{10} = \frac{18 - 11}{10} = \frac{7}{10} \end{aligned}$$

$$\begin{aligned} \frac{1}{8} - \frac{1}{6} \times \frac{3}{8} &= \frac{1}{8} - \frac{1}{16} \\ &= \frac{2 - 1}{16} = \frac{1}{16} \end{aligned}$$

$$\frac{\frac{2}{5} \div \frac{1}{2} \text{ of } \frac{4}{9} - 1\frac{1}{10}}{\frac{1}{8} - \frac{1}{6} \text{ of } \frac{3}{8}} = \frac{\frac{7}{10}}{\frac{1}{16}}$$

$$= \frac{7}{10} \times \frac{16}{1}$$

$$= \frac{56}{5} = 11\frac{1}{5}$$

$$4. \quad \text{a) } \angle DAC = \angle DCA = \frac{1}{2} (180 - 100) \text{ (base sios)} = 40^\circ$$

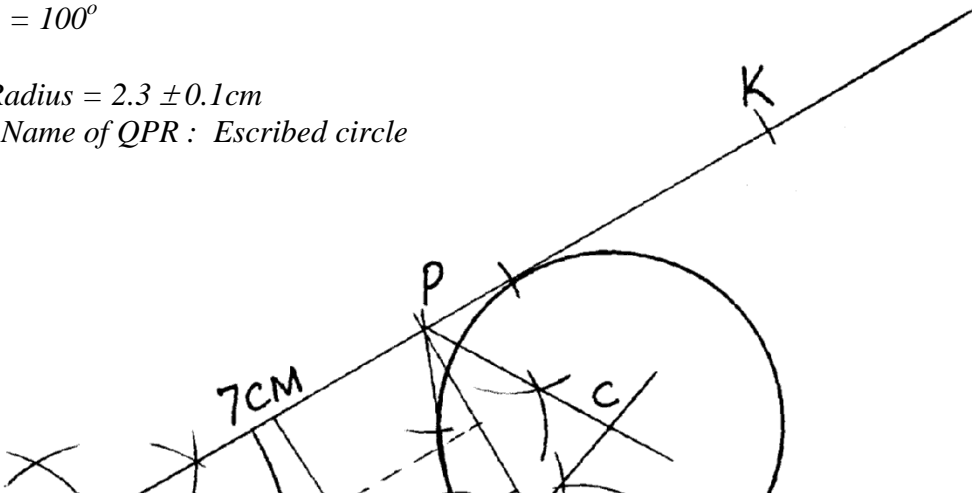
$$\begin{aligned} \text{(b) } \angle BAC &= \angle DCA \text{ alt } \angle \text{s AB//AD} \\ &= 40^\circ \end{aligned}$$

$$\text{(b) } \angle DAB = \angle DAC + \angle BAC = 40 + 40 = 80^\circ$$

$$\begin{aligned} \angle BCD &= 180^\circ - 80^\circ \\ &= 100^\circ \end{aligned}$$

$$5. \quad \text{c) (ii) Radius} = 2.3 \pm 0.1 \text{ cm}$$

Name of QPR : Escribed circle



6. (i) $\angle ACB = 10^\circ$ (\angle s subtended by chord AB)
(ii) $\angle AOD = 160^\circ$ (\angle at centre line at circumference)
(iii) $\angle CAB = 40^\circ$ (\angle s subtended by chord AB)
(iv) $\angle ABC = 130^\circ$ (Opposite \angle s of cyclic quadrilateral)
(v) $\angle AXB = 60^\circ$ (sum angle of triangle)

7. i) $\frac{80}{360} \times \frac{22}{7} \times 9 \times 9$
 $= 63.6429 \text{ cm}^2$

ii) $\frac{1}{2} ab \sin C$
 $= \frac{1}{2} \times 9 \times 9 \sin 80^\circ$
 $= 39.8847 \text{ cm}^2$

iii) $\frac{180}{360} \times \frac{22}{7} \times 9 \times 9$
 $= 127.2857 \text{ cm}^2$

Segment: $63.6429 - 39.8847$
 $= 23.7582 \times 2 = 47.5164 \text{ cm}^2$

$\therefore 127.2857 - 47.5164$
 $= 79.7693 \text{ cm}^2 = 79.77 \text{ cm}^2$

8. (a) $\angle RST = 180^\circ - 46^\circ$ Opposite angel in cyclic quadrilateral
 $= 134^\circ$

(b) $\angle SUT = 180^\circ - 46^\circ - 27^\circ$ (Sum of angles in a traingle QRU)
 $= 180^\circ - 173^\circ = 7^\circ$

(c) $\angle ROT = 2 \times 46^\circ$ (angle substended by chord RT at the centre)
 $= 92^\circ$

(d) $\angle PST = 180^\circ - 37^\circ - 48^\circ - 53^\circ$
Sum of angles in a triangle PST

(e) Reflex $\angle SOP = (2 \times 37^\circ) + 2 \times 42^\circ = 158^\circ$
Angle subtended chord at centres is twice angle at circle

9. $\angle POQ = 80^\circ$
Radius = $\frac{1.7}{\sin 40}$
 $= 2.645 \text{ cm}$
Area of the triangle = $\frac{1}{2} \times 2.645^2 \sin 80 = 3.445 \text{ cm}^2$
Area of the sector = $(\frac{80}{360} \times \pi \times 2.645^2)$
 $= 4.884 \text{ cm}^2$
Area of the shaded segment = $(4.884 - 3.445) = 1.439 \text{ cm}^2$

10. a) $\sphericalangle BDC = 90^\circ - 33^\circ$, 3rd angle of

$= 57^\circ \triangle BCD$, $\sphericalangle BCD = 90^\circ$.

$$\begin{aligned}\sphericalangle ADC &= \sphericalangle ADB + \sphericalangle BDC \\ &= 48^\circ + 57^\circ = 105^\circ\end{aligned}$$

b) Consider $\triangle BCE$

$\sphericalangle AEB$ is an exterior opposite angle

$$\therefore \sphericalangle AEB = 33^\circ + 48^\circ = 81^\circ \checkmark$$