

## 2. Common logarithms.

<b>1.</b>	$\text{Log } 31.59 = 1.4996$ $\text{Log } a = \underline{2.6182}$ $\text{Log } b^{1/3} = \underline{28.814}$ $\text{Log } b = \underline{\underline{3}}$ $\text{Log } b = \underline{4.6442}$ $b = 0.0004407$ $b = 0.0004$	<b>M1</b>	Subt b logs																																																												
		<b>M1</b>	Multip by 3																																																												
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		<b>04</b>																																																													
<b>2.</b>	$\text{Log}_{10}25 - \text{log}_{10}4 + \text{log}_{10}1600$ $\text{log}_{10}\left(\frac{25}{4} \times 1600\right)$ 4	<b>M1</b>																																																													
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<b>4</b>	$\frac{\text{log}\left(\frac{1}{4} \times 64\right)}{\text{log}\left(\frac{1}{32} \div \frac{1}{8}\right)}$ $\frac{\text{log } 2^4}{\text{log } 2^{-2}}$ $\frac{4 \text{ log } 2}{-2 \text{ log } 2}$ -2	M <sub>1</sub>																																																													
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5.  $\left(\frac{1}{2^3}\right)^x \cdot \left[2^6\right]^2 = \left[2^4\right]^2$  M1 for writing in index form

$2^{-3x} \cdot 2^{12} = 2^8$

$12 - 3x = 8$  M1

$$x = \frac{4}{3}$$

$$= 1\frac{1}{3}$$

3

6.	No.	std form	log		
	0.6845 <sup>2</sup>	6.845x10 <sup>-1</sup>	$\overline{1.8354} \times 2$		
	0.08416	8.416x10 <sup>-2</sup>	$\overline{1.6708} \quad \overline{1.6708}$		
			$\underline{\underline{2.9252}}$		
			3		
			$\overline{1.6417} \quad \overline{1.6417} +$	M1	
	0.005937	5.937x10 <sup>-3</sup>	$\overline{1.3125}$	M1	
		3.459x10 <sup>-1</sup>	$- \underline{\underline{3.7736}}$	M1	
	0.3459		$\overline{1.5389}$	A1	
			←		
				04	

7	Number	log		
	8.694	0.9392		M1
	0.1267	$\overline{1.1028} \times \frac{1}{3} = \overline{1.7009}$		M1
	0.006974	$\overline{3.8434}$		M1
		$\overline{3.5443} \times \frac{3}{4}$		M1
		$\overline{1.3861} \times 3 = \overline{2.1583}$		M1
		0.9392		M1
		$\overline{2.1583}$		M1
	6.039x10 <sup>2</sup>	$\underline{\underline{2.7809}}$		A1
	602.9			A1
				4 marks

8.

No.	Log
2849	3.4547
-	+
0.00574	3.7589
$\underline{\underline{1.2136}}$	←
36.891.1	1.5669
-	+
0.023	$\underline{\underline{2.3617}}$
	3.2052 →
2.0084 x 1/4	
3.178 x 10 <sup>-1</sup>	← 1.5021
→	0.3178

*All logs read correctly*

*Correct Addn /subst. of logs.*

$$9. \quad \begin{aligned} \log y &= \log B + n \log x \\ n \log x &= \log y - \log B \\ n &= \frac{\log (y/B)}{\log x} \end{aligned}$$

$$10. \quad \begin{aligned} &= 6 \log_2 4 + 10 \log_3 3 \\ &= 12 \log_2 2 + 10 \log_3 3 \\ &= 12 + 10 \end{aligned}$$

$$11. \quad \log \frac{2x-11}{2} = \frac{\log 3}{x}$$

$$\begin{aligned} (2x-11) &= \frac{3}{x} \\ 2x^2 - 11x - 6 &= 0 \\ (2x+1)(x-6) &= 0 \\ x &= -\frac{1}{2} \text{ or } 6 \\ x &= 6 \end{aligned}$$

12.

No.	Log
0.5241	T.7194
$(0.5241)^2$	T.7194x2
83.59	<u>T.4388</u> +
	1.9222
	1.3610
0.3563	T.5518
$3\sqrt{0.3563}$	$(3+2.5518) \div 3$
	T.8506
	0.3610 -
	1.8506
$3.239 \times 10^1$	1.5104
= 32.4	

$$13. \quad \begin{array}{r|l} \text{No.} & \text{Log} \\ \hline 38.32 & 1.5834 \\ 12.964 & \underline{1.1127} \\ & 2.6961 \\ 86.37 & 1.9364 \\ 6.285 & \underline{0.7783} \\ & 2.7347 \\ - & 1.9587 \\ \hline & \underline{-\bar{3} + 2.9587} = 1.9866 \\ & 3 = 0.9695 \end{array}$$

$$14. \quad \begin{aligned} H^3 &= \frac{3d(L-d)}{10L} \\ \sim 3dL - 10H^3L &= 3d^2 \\ \sim L(3d - 10H^3) &= 3d^2 \\ L &= \frac{3d^2}{3d - 10H^3} \end{aligned}$$

15.	No.	Log
	6.195	0.7920
	11.82	<u>1.0726</u>
		1.8646
	83.52	<u>1.9218</u>
		<u>1.9428 x 1/4</u>
		4. + 3.9428
		4
	0.9676	<u>1.9857</u>

16.  $\log y^2 (x-1) = \log 9 y^2 (x-1) = 9 \dots(1)$   
 $\log (xy) \log 6 xy = 6 \dots 2$   
from (2)  $x = 6/y$   
substitute in (1)  $y(6 - 1) = 9$   
 $y$   
 $6y - y^2 = 9$   
 $y^2 - 6y + 9 = 0$   
 $(y-3)^2 = 0$   
 $y = 3$   
 $\therefore x = 2$

17.  ${}^{4/5} \log_{10} 25 + \log_{10} 25x^2 - \log 10$   
 $4 \log 2 = \log_{10} 25x^2 - 3 \log 2$   
 $2 \log 10 + 2 \log 5$   
 $\log 10 \times 100$

18.

NO	LOG
0.9895	-
$(0.9895)^2$	<u>1.9954</u>
	1.9954 x 2
	1.9908
0.004974	-
	3.6968
	<del>3.6876</del> ÷ 4
6.598	1.4219 x 3
	2.2657
	0.8195 -
	2.2657
$3.579 \times 10^2$	2.5538
OR 357.9	

Use sine rule

$$19. \text{Log } 3x + 8 - \log 8 = \log (x-4)$$

$$\text{Log } \frac{(3x + 8)}{8} = \log (x-4)$$

$$3x + 8 = x - 4$$

$$3x + 8 = 8x - 32$$

$$5x = 40$$

20.

No.	Log
36.72 $\longrightarrow$	1.5649
0.46 <sup>2</sup> $\longrightarrow$	2(T.6628)
	<u>T.3256</u>
185.4	0.8905
	<u>2.2682</u>
	2.9223 x $\frac{1}{3} = \frac{2}{3} + \frac{1.6223}{3}$
3.474 x 10 <sup>-1</sup>	-
Or 0.3474	<u>1.5408</u>

21.

No	Log
Sin 44.5	1.8457
Tan 14.9	1.4250
Cos 82	1.1486 +
	$\frac{1.2772}{2}$
10 x 4.351	_____ 0.6386

22. From square roots  $12.25 = 3.5$

$$\frac{3.264 \times 1.215 \times 3.5 \times \sqrt{107}}{1.088 \times 0.4725 \times 107}$$

$$\frac{3264 \times 1215 \times 35}{1088 \times 4725}$$

$$\sqrt{27} = 3$$

23.  $\text{Log}_8(x + 5) - \log_8(x - 3) = \text{Log}_8 4$

$$\text{Log}_8 \frac{(x + 5)}{x - 3} = \log_8 4$$

$$\frac{x + 5}{x - 3} = 4$$

$$x - 3$$

$$4x - 12 = x + 5$$

$$3x = 17$$

$$x = 17 = 5^{2/3}$$

$$\text{Or } \log_8 \frac{x + 5}{x - 3} = \frac{2}{3}$$

$$8^{2/3} = \frac{x + 5}{x - 3}$$

$$2^3(2/3) = \frac{x + 5}{x - 3}$$

$$2^2 = \frac{x + 5}{x - 3} \Rightarrow 4 = \frac{x + 5}{x - 3}$$

$$4x - 12 = x + 5 \Rightarrow 3x = 17$$

$$x = \frac{17}{3} = 5\frac{2}{3}$$

24.

<p>No  <math>6.57^2</math></p> <p><math>4.317 \times 10^1</math>  <math>43.17 + 6.57</math></p> <p>49.74  <math>(7.92)^2</math></p> <p><math>\frac{30.08}{2.636 \times 10^{-2}}</math></p>	<p>Log  0.8176  <u>2x</u>  <u>1.6352</u></p> <p>1.6967</p> <p>0.8987  <u>X2</u>  1.7974</p> <p>1.4783 + <math>\frac{3.2757}{2.4210}</math>  = 0.02636  = 0.0264 (4 d.p)</p>
<p>No  <math>6.57^2</math></p> <p><math>4.317 \times 10^1</math>  <math>43.17 + 6.57</math></p> <p>49.74  <math>(7.92)^2</math></p> <p><math>\frac{30.08}{2.636 \times 10^{-2}}</math></p>	<p>Log  0.8176  <u>2x</u>  <u>1.6352</u></p> <p>1.6967</p> <p>0.8987  <u>X2</u>  1.7974</p> <p>1.4783 + <math>\frac{3.2757}{2.4210}</math>  = 0.02636  = 0.0264 (4 d.p)</p>

25.  $\log 120 = \log 4 + \log 3 + \log 10$   
 $= \log 2^2 + \log 3 + \log 10$   
 $= 2\log 2 + \log 3 + \log 10$   
 $= 2(0.30103) + 0.47712 + 1$   
 $= 2.07918$

26.  $\log_2 (3x - 4) = \frac{1}{3} \log_2 8x^6 - \log_2 4$   
 $\log_2 (3x - 4) = \log_2 (2^3 x^6) - \log_2 4$   
 $\log_2 (3x - 4) = \log_2 2x^2 - \log_2 4$

$$\log_2(3x-4) - \log_2\left(\frac{2x^2}{4}\right)$$

$$= 3x - 4 = \frac{2x^2}{4}$$

$$2x^2 - 12x + 16 = 0$$

$$x^2 - 6x + 8 = 0$$

$$x - 2x - 4x + 8 = 0$$

$$(x-2)(x-4) = 0$$

$$x = 2 \text{ or } x = 4$$

27.

No 5.627 (0.234) <sup>3</sup>	Log 0.7503 T. 3692 <u>    x 3</u> 2.8579
8.237	0.4779 <u>0.9158</u> 2
2.399 x 10 <sup>-3</sup>	3.3800  = 0.002399

28. Det 2 - -3 = 5  
Area of A<sup>1</sup>B<sup>1</sup>C<sup>1</sup> = 5 x 15  
= 75 cm<sup>2</sup>

29.  $\log_{10}(6x-2) - \log_{10} = \log_{10}(x-3)$   
 $\log \frac{(6x-2)}{10} = \log (x-3)$   
 $\frac{6x-2}{10} = x-3$   
 $6x-2 = 10x-30$   
 $x = 7$

30. No.                      Log  
0.07526<sup>2</sup>              2.8766 x 2 = 3.7532  
6.652                    0.8230 = 0.8230  
                                  4.9302

$$\frac{4.9302}{3} = 6 + \frac{2.9302}{3}$$

$$= 2.9767$$

$$\text{Antilog} = 9.4776 \times 10^{-2}$$

$$= 0.094776(\text{accept } 0.09478)$$

<i>No.</i>	<i>Log</i>
4.283	<u>0.6317</u>
$0.009478^2$	<u><math>3.9767 \times 2 +</math></u>
	<u>5.9534</u>
	<u>4.5851 -</u>
<i>Log</i> 9.814	<u>1.9964</u>
	<u><math>4.5887 \div 5</math></u>
$2.0785 \times 10^{-1}$	<u>1.3177</u>
$= 0.20785$	