

2. Fractions

1	$\frac{(5)^{3 \times \frac{2}{3}} \div 3^4}{3^{-\frac{3}{5} \times 5}} = \frac{5^2 \div 3^4}{3^{-3}}$ $= 5^2 \div 3^7$ $= \frac{25}{2187}$	<p>M₁</p> <p>M₁</p> <p>A₁</p>	<p>Simplifying numerator</p> <p>simplify</p>
2.	$\text{Num} \left(\frac{1}{5} \times 20 \right)^{\frac{1}{2}}$ $= 4^{\frac{1}{2}}$ $= 2$ <p>Denom. 8 x 1 x 25</p> $= 200$ $= \frac{2}{200}$ $\frac{1}{100}$	<p>M1</p> <p>M1</p> <p>A1</p>	<p>Or equivalent 0.01</p>
		03	
3.	$\frac{\left(\frac{10}{7} - \frac{5}{8} \right) \times \frac{2}{3}}{\frac{3}{4} + \frac{12}{7} \times \frac{7}{4} \times \frac{7}{3}}$ $\frac{\frac{45}{56} \times \frac{2}{3}}{\frac{3}{4} + 1}$ $\frac{\frac{15}{28}}{\frac{7}{4}}$ $\frac{15}{28} \times \frac{4}{7} = \frac{15}{49}$	<p>M1</p> <p>M1</p> <p>A1</p>	<p>✓ Application of bodmas</p> <p>Simplification of both numerators and denominator</p>

	$\left(\frac{10^5}{3^5}\right)^{\frac{2}{5}} \times \left(\frac{3^2}{10^4}\right)^{\frac{1}{2}}$ $\frac{100}{9} \times \frac{3}{100}$ $\frac{1}{3}$	<p>M₁</p> <p>M₁</p> <p>$\frac{A_1}{3}$</p>	
8.	$\frac{\frac{6}{7} \text{ of } \frac{14}{3} \div 80 \times -\frac{20}{3}}{-2 \times 5 + (14 \div 7) \times 3}$ $\frac{4 \div 80 \times -\frac{20}{3}}{-2 \times 5 + 2 \times 3}$ $\frac{\frac{1}{20} \times -\frac{20}{3}}{-10 + 6}$ $\frac{-\frac{1}{3}}{-4}$ $\frac{1}{3} \times \frac{1}{4} = \frac{1}{12}$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p>	
		04	
9.	<p>Let the number of chicken be x</p> <p>Turkeys will be x + 6</p> $\frac{1}{4}x + \frac{1}{3}(x + 6) = 30$ $\frac{1}{4}x + \frac{1}{3}x + 2 = 30$ $\frac{7}{12}x = 28$ $= 48$ <p>Number of chickens = 48</p> <p>Number of turkeys = 48 + 6 = 54</p> <p>Total number of birds = 54 + 48</p> $= 102$	<p>B1</p> <p>B1</p>	<p>For 48</p> <p>For 102</p>

$$11. \quad \frac{-4 \text{ of } (-4 - 3) + -3 - 2}{-12 + 3 + 5}$$

$$\frac{-4 \text{ of } (-7 - 3 - 2)}{-4}$$

$$= \frac{48}{-4}$$

$$= -12$$

M1

for -4

M1

for 48

A1

3

12.

(a) (i) ratio

$$r = \frac{3}{100} \div \frac{3}{10}$$

$$r = \frac{3}{100} \times \frac{10}{3} = \frac{1}{10}$$

$$ii) S_n = \frac{\frac{3}{10} \left(1 - \frac{1}{10}\right)^{n-1}}{1 - \frac{1}{10}}$$

$$S_n = \frac{\frac{3}{10} \left(\frac{9}{10}\right)^{n-1}}{\frac{9}{10}}$$

$$S_n = \frac{3}{10} \times \frac{10}{9} \left(\frac{9}{10}\right)^{n-1}$$

$$S_n = \frac{1}{3} \left(\frac{9}{10}\right)^{n-1}$$

$$iii) T_8 = \frac{3}{10} \left(\frac{1}{10}\right)^{8-1}$$

$$= \frac{3}{10} \left(\frac{1}{10}\right)^7$$

$$= \frac{3}{10} \times \frac{1}{10^7} = \frac{3}{100,000,000}$$

(b) 1st bounce 30m

$$2^{\text{nd}} \frac{3}{4} \times 30 = 22.5\text{m}$$

$$3^{\text{rd}} \frac{3}{4} \times 22.5 = 16.85\text{m}$$

$$4^{\text{th}} \frac{3}{4} \times 16.85 = 12.64\text{m}$$

$$5^{\text{th}} \frac{3}{4} \times 12.64 = 9.48\text{m}$$

$$6^{\text{th}} \frac{3}{4} \times 9.48 = 7.11\text{m}$$

$$7^{\text{th}} \frac{3}{4} \times 7.11 = 5.3325\text{m}$$

$$8^{\text{th}} \frac{3}{4} \times 5.3325 = 3.9993\text{m}$$

$$9^{\text{th}} \frac{3}{4} \times 3.9993 = 2.9995\text{m}$$

$$10^{\text{th}} \frac{3}{4} \times 2.9995 = 2.2496\text{m} \approx 2.25$$

Or using formula

$$T_{10} = 30 \left(\frac{3}{4}\right)^{10-1} = 30 \left(\frac{3}{4}\right)^9$$

$$= 30 \times 0.07508$$

$$\approx 2.2524\text{m} \approx 2.25\text{m}$$

M1

A1

M1

M1

A1

M1

A1

M1

M1

Every four

M1

Every four

A1

2 d.p

M1

A1

13.	$\frac{5}{\frac{12}{43} = \frac{25}{43}}$ $\frac{20}{43}$	M1 M1 A1	For num For den
		03	
14.	<i>Numerator</i> $\rightarrow 7 + -6 = 1$ <i>Denominator</i> $\rightarrow -9 + 2 + 4 = -3$ $= -\frac{1}{3}$	M1 M1 A1	
		03	

1615	$\sqrt[3]{13824}$ $\sqrt[3]{13824} = 24$ $\sqrt[3]{13824} = 24$ $\sqrt[3]{13824} = 24$ $\sqrt[3]{13824} = 24$ $13824 = \sqrt[3]{2^9 \times 3^3} = 2^3 \times 3^1 = 24$ $24 = 2 \times 2 \times 2 \times 3$ $\frac{-30}{3}$	M1 <u>A1</u> 2	Numerators & Denominators M1 M1 A1	Simplified denominator $\sqrt[3]{}$ Method shown Show how to get factors of 13824
			3 marks	

17	$100r = 193.\dot{3}\dot{3}\dots$ $10r = 19.\dot{3}\dot{3}\dots$ <hr style="width: 40%; margin: 0 auto;"/> $90r = 174$ $r = \frac{174}{90}$ $100r = 25.\dot{2}\dot{5}\dots$ $r = 0.\dot{2}\dot{5}\dots$ <hr style="width: 40%; margin: 0 auto;"/> $99r = 25$ $r = \frac{25}{99}$ $\frac{174}{90} + \frac{25}{99}$ $= \frac{2164}{990}$ $= 2\frac{92}{445}$	B1	
		B1 B1	
		3	

18. $\frac{1}{2} \times \frac{7}{2} = \frac{3}{2} \times \frac{1}{6} \quad \frac{3}{4} \times \frac{5}{2} \times X$

$$\frac{7}{4} + \frac{3}{2} \times \frac{11}{2} = \frac{15}{4}$$

$$\frac{7}{4} + \frac{11}{4} = \frac{18}{4}$$

B1

$$\therefore \frac{18}{4} \div \frac{15}{4}$$

$$\frac{18}{4} \times \frac{4}{15} = \frac{6}{5} = 1\frac{1}{5}$$

A1

19. $\frac{2}{5} \div \frac{1}{2} \text{ of } \frac{4}{9} - 1\frac{1}{10}$

$$= \frac{2}{5} \div \frac{1}{2} \times \frac{4}{9} - \frac{11}{10}$$

$$= \frac{2}{5} \times \frac{9}{2} - \frac{11}{10}$$

$$= \frac{9}{5} - \frac{11}{10} = \frac{18-11}{10} = \frac{7}{10}$$

$$\frac{1}{8} - \frac{1}{6} \times \frac{3}{8} = \frac{1}{8} - \frac{1}{16}$$

$$= \frac{2-1}{16} = \frac{1}{16}$$

$$\frac{\frac{2}{5} \div \frac{1}{2} \text{ of } \frac{4}{9} - 1\frac{1}{10}}{\frac{1}{8} - \frac{1}{6} \text{ of } \frac{3}{8}} = \frac{\frac{7}{10}}{\frac{1}{16}}$$

$$= \frac{7}{10} \times \frac{16}{1}$$

$$= \frac{56}{5} = 11\frac{1}{5}$$

20. **BODMAS**

$$\frac{3}{7} \times \frac{7}{3} = 1$$

$$\frac{9}{7} \times 1 = \frac{9}{7}$$

$$\frac{3}{4} + \frac{9}{7} = 21 + 36 = 57$$

M1

$$\frac{28}{7} - \frac{28}{8} = 72 - 21 = 51 \times \frac{2}{3} = \frac{17}{28}$$

M1

$$\frac{57}{28} \times \frac{28}{17} = 3\frac{6}{17}$$

A1

$$\begin{aligned}
 21. \quad & \frac{\frac{2}{5}x - \frac{9}{2} - \frac{11}{10}}{\frac{1}{8} - \frac{1}{16}} \\
 & = \frac{7}{10}x - \frac{16}{1} \\
 & = \frac{56}{5} = 11\frac{1}{5}
 \end{aligned}$$

$$\begin{aligned}
 22. \quad & \frac{3}{8} \left(\frac{38}{5} - \frac{55}{36}x^{12/5} \right) \\
 & \frac{3}{8}x^{59/15} = \frac{59}{40} = 1\frac{19}{40}
 \end{aligned}$$

$$\begin{aligned}
 23. \quad & \text{Numerator} \\
 & \frac{\left(\frac{9}{5}x^{25/18} \right) \div \frac{5}{2}x^{24}}{\frac{7}{3} - \left(\frac{1}{4}x^{12} \right) \div \frac{5}{3}} \\
 & \frac{9}{5}x^{25/18} = \frac{5}{2} \div \frac{5}{3}x^{24} \\
 & \frac{5}{2}x^{3/5}x^{24} = 36 \\
 & \frac{7}{3} - \frac{1}{4}x^{12} \div \frac{5}{3} \\
 & \frac{7}{3} - 3x^{3/5} \\
 & \therefore \frac{36}{8/15} = 67.50 \\
 & \frac{8}{15} = 67\frac{1}{2} \\
 & \frac{7}{3} - 3x^{3/5}
 \end{aligned}$$

$$\begin{aligned}
 24. \quad & \text{Let } X \text{ be money raised} \\
 & \text{Teachers house} = \frac{1}{7}x \\
 & \text{Classrooms} = \frac{2}{3}x^{6/7} = \frac{4}{7}x \\
 & \text{Remainder} = \frac{1}{3}x^{6/7} = \frac{2}{7}x \\
 & \frac{2}{7}x = 300000 \\
 & x = \text{Shs. } 1050000
 \end{aligned}$$