121/2

280

S

913022

MATHEMATICS ALT A

Mar. 2022 - 21/2 hours

Paper 2



Na	me					\.	لورد	/		Ind	ex N	umb	er	· · · · · · · · · · · · · · · · · · ·	
Ca	ndidate	e's Si	igna	ture	M		رور ر			_					
Ins	tructio	ns to	can	dida	tes	7 . p/30	7. 14.0	ise e	003.3	27					
(b) S (c) T (d) A	Write you Sign and this pape Answer al	write the constant	he date ists of ruestic	e of ex two se ons in S	amina ection Section	ition ii s: Sec o n I ar	n the s tion I nd only	paces and So five	provide provid	ied ab II. Ons fro	ove. m Sec			<i>1</i> _ 43_	
(f) N	how all paces be farks may	elow e be gi	each q	ruesti r corre	on. ect wo	rking	even i	f the a	nswer	is wro	ng.		-1,	7.6	
(h) T . (i) C	ion-prog sed excer his pape andidate rinted as andidate	ot wheer con es sho indic	re states ould class	ed oth of 19 p heck t and t	erwise printe the qu hat no	e. ed paguestic o que	ges. on pay	per to	asce: missi:	rtain (17			700	
For E Secti	xamin on I	er's	Use (Only										į	
1	2.3	4	5	6	7	8	9	10	11	12	13	14	15	163	Total
	# <u>.</u>					Ì					. 19 ***			Ď.	
	Sect	ion	ΙΙ	•							3+ :		3	ў Г	
	17	18	19		21		23 			\dashv	es	ran	d To	tal	
			•	- C 2	h'Ogy	rea	7 ES	NEI (833 B	(5.7)**					

© 2021 The Kenya National Examinations Council 121/2



Turn over

Download this and other FREE materials from https://teacher.co.ke/notes



SECTION I (50 marks)

Answer all the questions in this section in the spaces provided.

An empty tank of capacity 18480 litres is to be filled with water using a cylindrical pipe of 1. diameter 0.028 m. The rate of flow of water from the pipe is 2 m/s. Find the time in hours it would take to fill up the tank. (Take $\pi = \frac{22}{7}$).

The first term of a Geometric Progression (G.P) is 2. The common ratio of the G.P is also 2. The product of the last two terms of the G.P is 512. Determine the number of terms in the G.P. 2. (3 marks)

Last term =
$$2(2^{n-1})$$
 = $3(2^{n-3})$ The expression $3(2^{n-3})$ = $3(2^{n-3}$

3. (2 marts)

Aff. 1
Using diveriminant:

$$b^2 = 4ac$$

 $(-30)^2 = 4(9)(9)$
 $\Rightarrow 0 = 25$

Let
$$ax^{2}-36x+9=(Kx-b)^{2}$$
 $ax^{2}-36x+9=(Kx-b)^{2}$
 $ax^{2}-30x+9=K^{2}x^{2}-3Kbx+b^{2}$
Comparing,
 $q=b^{2}\Rightarrow b=\pm 3$
And $30=2Kb\Rightarrow k=\pm 5$
And $q=k^{2}\Rightarrow q=25$

Make x the subject of the formula $y = \frac{bx}{\sqrt{cx^2 - a}}$. 4.

Squaring both sides,
$$y^2 = \frac{b^2 x^2}{cx^2 - a}$$

$$\Rightarrow y^2(cx^2 - a) = b^2 x^2$$

Squaring both sides,

$$y^{2} = \frac{b^{2}x^{2}}{cx^{2}-q}$$

$$\Rightarrow y^{2}cx^{2}-b^{2}x^{2} = qy^{2}$$

$$\Rightarrow y^{2}(cx^{2}-q) = b^{2}x^{2}$$

$$\Rightarrow y^{2}(cx^{2}-q) = b^{2}x^{2}$$

$$\Rightarrow y^{2}(cx^{2}-q) = b^{2}x^{2}$$

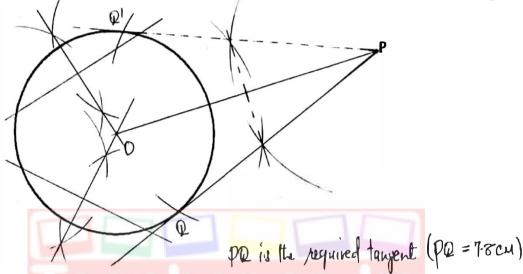
$$\Rightarrow y^{2}(cx^{2}-d) = b^{2}x^{2}$$

$$\Rightarrow y^{2}(cx^{2}-d) = b^{2}x^{2}$$

$$\Rightarrow y^{2}(cx^{2}-d) = ay^{2}$$

$$\Rightarrow x^{2} = \frac{ay^{2}}{cy^{2}-b^{2}}$$
below shows a circle and a point P outside the circle

5. The figure below shows a circle and a point P outside the circle



Using a ruler and pair of compasses, construct a tangent to the circle from P.

(4 marks)

6. Four quantities P, Q, R and S are such that P varies directly as the square root of Q and inversely as the square of the difference of R and S. Quantity Q is increased by 44% while quantities R and S are each decreased by 10%.

Find the corresponding percentage change in P correct to 1 decimal place.

(4 marks)

$$P\alpha \frac{\sqrt{Q}}{(R-S)^{2}} \Rightarrow P = \frac{k\sqrt{Q}}{(R-S)^{2}}$$

$$P' = \frac{k\sqrt{1.44Q}}{[0.9(R-S)]^{2}}$$

$$= \frac{1.2}{0.9^{2}} \frac{k\sqrt{Q}}{(R-S)^{2}}$$

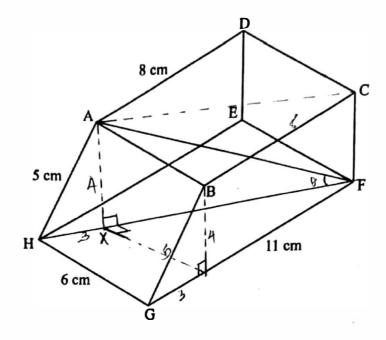
$$\Rightarrow P' = \frac{40}{27}P$$
Kenya Certificate of Secondary Education, 2021

913022

Turn over



7. The figure below represents a prism ABCDEFGH of length 6 cm. The cross section BCFG of the prism is a trapezium in which GF = 11 cm, BC = 8 cm, BG = 5 cm and \angle GFC = \angle BCF = 90°.



Calculate correct to 1 decimal place the angle between the line FA and the plane GFEH.

FH =
$$\sqrt{6^2 + 11^3} = \sqrt{157}$$
 tan $\alpha = \frac{4}{\sqrt{157} - 3}$
 $\theta \approx 22.8^{\circ}$

(or $\theta \approx 21.8^{\circ}$ if $Fx = Ac = 10$ cm is used)

8. The cash price of a gas cooker is Ksh 20 000. A customer bought the cooker on hire purchase terms by paying a deposit of Ksh 10 000 followed by 18 equal monthly instalments of Ksh 900 each. Annual interest, compounded quarterly, was charged on the balance for the period of 18 months. Determine, correct to 1 decimal place, the rate of interest per annum. (4 marks)

$$\dot{A} = P(1 + \sqrt{100})^{1}$$

$$(18x 900) = (20000 - 10000)(1 + \sqrt{400})^{1}$$

$$6\sqrt{16200} = (1 + \sqrt{400})$$

$$\dot{Y} = (6\sqrt{1.62} - 1) \times 400$$

$$\dot{Y} = 33.56 \text{ Merbya Certificate of Secondary Education, 2021}$$

$$13022 = 33.56 \text{ Merbya Certificate of Secondary Education, 2021}$$

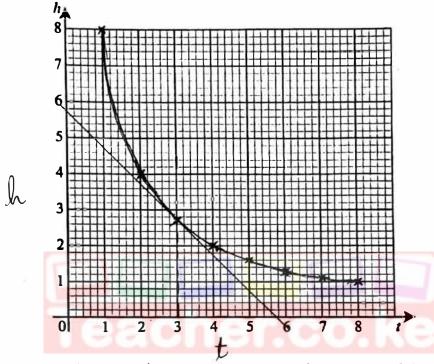


9. The table below shows the values of t and the corresponding values of h for a given relation.

X	t	1	2	3	4	5	6	7	8
7	h	8	4	2.7	2	1.6	1.3	1.1	1

(a) On the grid provided, draw a graph to represent the information on the table given.

(2 marks)



(b) Use the graph to determine, correct to 1 decimal place, the rate of change of h at t = 3. (2 marks)

Note of change = gradient at
$$t = 3$$

$$= \frac{47}{4x}$$

$$= 0-5.7$$

$$= -1.0$$



- 10. The equation of a trigonometric wave is $y = 4 \sin (ax - 70)^{\circ}$. The wave has a period of 180°.
 - (a) Determine the value of a.

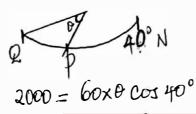
(1 mark)

$$\frac{360}{9} = 180^{\circ} \implies 9 = 2$$

(b) Deduce the phase angle of the wave. (1 mark)

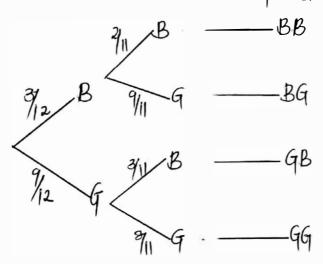
$$\left|-70^{\circ}\right| \Rightarrow 70^{\circ}$$

A point Q is 2000 nm to the West of a point P(40°N, 155°W). Find the longitude of Q to the 11. (3 marks) nearest degree.



- 12. A box contains 3 brown balls and 9 green balls. The balls are identical except for the colours. Two balls are picked at random without replacement.
 - Draw a tree diagram to show all the possible outcomes.

 Paisible outcomes: (1 mark) (a)



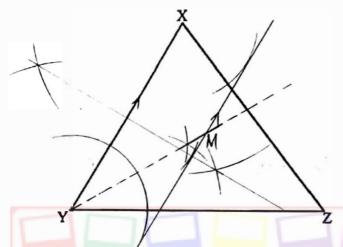


(b) Determine the probability that the balls picked are of different colours.



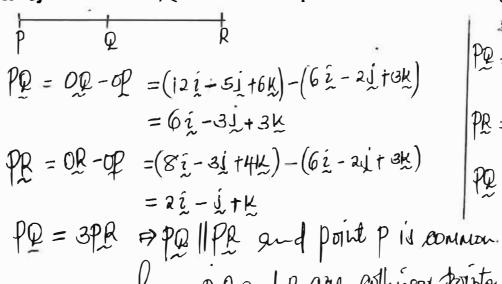
$$P(BG) = 06 P(GB)$$
 $(\frac{3}{1} \times \frac{3}{1}) + (\frac{3}{1} \times \frac{3}{1})$
 $\frac{54}{132} = 07 = \frac{9}{22}$

13. The figure below shows triangle XYZ.



Using a ruler and a pair of compasses, locate a point M on the triangle such that M is 2 cm from line YX and is equidistant from lines YX and YZ. Measure length YM. (3 marks)

The position vectors of points P, Q and R are OP = 6i - 2j + 3k, OQ = 12i - 5j + 6k and 14. OR = 8i - 3j + 4k. Show that P, Q and R are collinear points. (3 marks)



Kenya Certificate of Secondary Education, 2021 121/2

Turn over

 $\begin{array}{c}
PR = \begin{pmatrix} 8 \\ -3 \\ + \end{pmatrix} - \begin{pmatrix} 6 \\ -2 \\ -1 \\ \end{pmatrix} \\
PQ = 3 PR
\end{array}$



15. In a transformation an object of area x cm² is mapped on to an image whose area is 13x cm².

Given that the matrix of the transformation is $\begin{pmatrix} x & 7 \\ x-1 & 3x \end{pmatrix}$, find the possible values of x. (3 marks)

ASF = det 7 frant. =
$$\frac{A \cdot 0}{A \cdot 0}$$
 Image
A of Object

$$\Rightarrow x(3x) - 7(x-1) = \frac{13x}{x} = 13$$

$$\Rightarrow 3x^2 - 7x + 7 - 13 = 0$$

$$\Rightarrow 3x^2 - 9x + 2x - 6 = 0$$

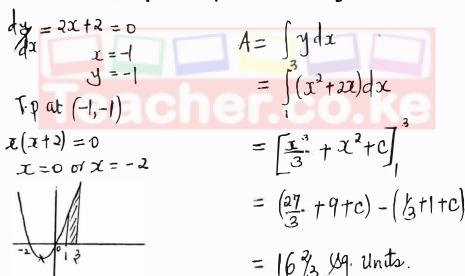
$$\Rightarrow 3x^2 - 9x + 2x - 6 = 0$$

$$\Rightarrow (x-3)(3x+2) = 0$$

$$\Rightarrow x-3 = 0 \text{ or } 3x+2 = 0 \Rightarrow x = 3 \text{ or } x = -\frac{9}{3}$$

Find the area enclosed by the curve $y = x^2 + 2x$ the straight lines x = 1, x = 3 and the x-axis.

(3 marks)



Download this and other FREE materials from https://teacher.co.ke/notes



SECTION II (50 marks)

Answer only five questions in this section in the spaces provided.

- 17. Pump P can fill an empty water tank in $7\frac{1}{2}$ hours while pump Q can fill the same tank in $11\frac{1}{4}$ hours. On a certain day, when the tank was empty, both pumps were opened for $2\frac{1}{2}$ hours.
 - (a) Determine the fraction of the tank that was still empty at the end of the $2\frac{1}{2}$ hours.

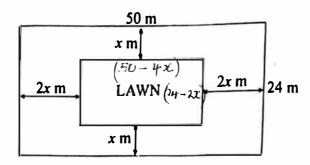
(b) Pump P was later opened alone to completely fill the tank. Determine the time it took pump P to fill the remaining fraction of the tank. (2 marks)

(c) The two pumps P and Q are operated by different proprietors. Water from the full tank was sold for Ksh 15 750. The money was shared between the two proprietors in the ratio of the quantity of water supplied by each.

Determine the amount of money received by the proprietor of pump P. (4 marks)



18. A rectangular plot measures 50 m by 24 m. A lawn, rectangular in shape, is situated inside the plot with a path surrounding it as shown in the figure below.



The width of the path in x m between the lengths of the lawn and those of the plot and 2x m between the widths of the lawn and those of the plot.

(a) Form and simplify an expression in x for the area of the:

(2 marks)

(1 mark)

$$(50\times24)-(8x^2-196x+1200)$$



- (b) The area of the path is $1\frac{1}{2}$ times the area of the lawn.
 - (i) Form an equation in x and hence solve for x.

(4 marks)

$$-81^{2}+196x = 1.5(8x^{2}-196x+1200)$$

$$-20x^{2}+490x-180 = 0$$
of $22^{2}-49x+180 = 0$

$$(2x-9)(x-20) = 0$$

$$2x-9 = 0 \text{ of } x-20 = 0$$

$$\Rightarrow x = 4/2 \text{ or } x = 20$$

(ii) Determine the perimeter of the lawn.

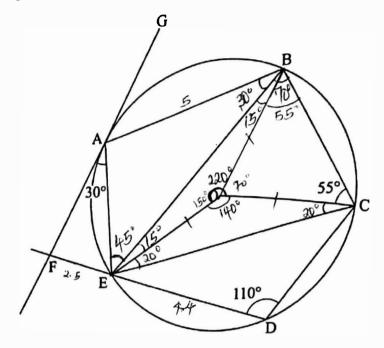
(3 marks)

appropriate value of
$$x = 4\frac{1}{2}$$

Length of brun = $50 - 4x + 6 = 32M$
Width of lawn = $24 - 2x + 6 = 15M$
Persineter = $2(32 + 15) = 94M$



In the figure below, points A, B, C, D and E lie on the circumference of a circle centre 0. In the figure below, points A, B, C, D and E lie on the circle is produced to intersect with the circle at A. Chord DE of the circle is produced to intersect with the 19. tangent at F. Angle FAE = 30° , \angle EDC = 110° and \angle OCB = 55° .



(a) Determine the size of:

(i)
$$\angle AEC. = |80^{\circ} - (70 + 30)^{\circ}$$

(3 marks

(ii)
$$\angle AEB. = 80^{\circ} - (20 + 15)^{\circ}$$

= 4.5°

(3 marks

- Given that AB = 5 cm, ED = 4.4 cm and FE = 2.5 cm. Calculate correct to 1 decimal (b) place:
 - the radius of the circle. (i)

(2 mark

$$5/2 = 2R$$

$$5/45 = 3.5 \text{ cm}$$
the length of line AF.

(ii)

(2 mark



The table below shows income tax rates in a certain year. 20.

Monthly taxable income in Kenya shillings	Tax rates
0 – 12 298	10%
12 299 – 23 885	15%
23 886 – 35 472	20%
35 473 – 47 059	25%
47 060 and above	30%

In the year, the monthly carnings of Kanini were as follows:

Basic salary

Ksh 64 500

House allowance

Ksh 12 000

Kanini contributes 7.5 % of her basic salary to a pension scheme. This contribution is exempted from taxation. She is entitled to a personal tax relief of Ksh 1 408 per month.

Calculate:

(a) Kanini's monthly taxable income. (2 marks)

280

$$= 64500 + 12000 = 75 \times 64500$$

$$= \text{Koh } 71662.50$$

$$= Ksh 7/662.50$$
the tax payable by Kanini that month. (6 marks)

$$| ^{8} | \text{band} : | 0 \% \times | 2.298 = Ksh 1 229.80$$

$$| ^{18} | \text{band} : | 15 \% \times | 1587 = Ksh 1 738.05$$

$$| ^{18} | \text{band} : | 20 \% \times | 1587 = Ksh 2 317.40 + \text{pth band} : | 25 \% \times | 1587 = Ksh 2 896.75$$

$$| ^{18} | \text{band} : | 30 \% \times 24603.60 = Ksh 7.381.05$$

$$| ^{18} | \text{band} : | 30 \% \times 24603.60 = Ksh 7.381.05$$

$$| ^{18} | \text{band} : | 30 \% \times 24603.60 = Ksh 7.381.05$$

$$| ^{18} | \text{band} : | 30 \% \times 24603.60 = Ksh 7.381.05$$

$$| ^{18} | \text{band} : | 30 \% \times 24603.60 = Ksh 15.563.05$$

$$| ^{18} | \text{band} : | 30 \% \times 24603.60 = Ksh 15.563.05$$

$$| ^{18} | \text{band} : | ^{18} | \text{band} :$$

(c)

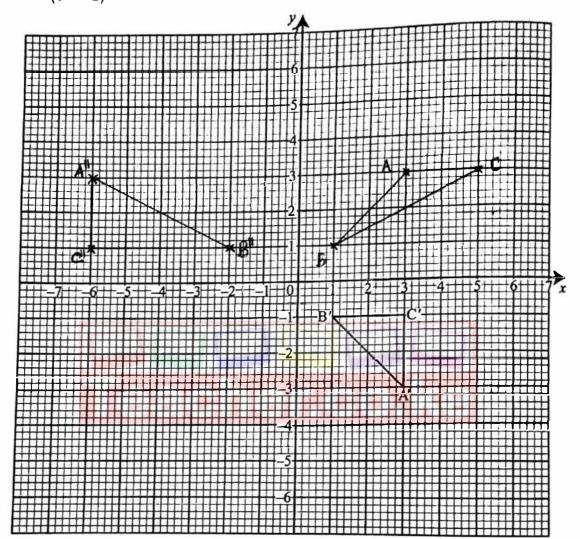
Net tax = KSh 14 155.05 Pension = $\frac{16h + 837.50}{164}$ Total deductions = KSh 18 992.55

Net pay = 76 500-18 992.55 = KCL 57 507.45





The vertices of the triangle shown on the grid are A'(3,-3), B'(1,-1) and C'(3,-1). 21. Triangle A'B'C' is the image of triangle ABC under a transformation whose matrix is $\begin{pmatrix} 0 & 1 \\ 1 & -2 \end{pmatrix}$.



Find the coordinates of triangle A, B and C.

(4 marts)

$$\Rightarrow A(3,3), B(1,1), C(5,3)$$

913022 A + 2 A + B + C + 2 A + B + C + 2 A + B + C + 2 A + B + C + 2 A + B + C + 2 A + 2 A + C + 2 A + 2 A + C + 2 A + C + 2 A + C + 2 A + C + 2 A + C + 2 A + C + 2 A + C + 2 A + C + 2 A + C + 2 A + C + 2 A + 2Kenya Certificate of Secondary Education, 2021



(b) Triangle A"B"C" is the image of triangle A'B'C' under a transformation matrix

$$\begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix}$$

(2 marks)

Determine the coordinates of A", B" and C".

$$\begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} 3 & 1 & 3 \\ -3 & -1 & -1 \end{pmatrix} = \begin{pmatrix} -6 & -2 & -6 \\ 3 & 1 & 1 \end{pmatrix}$$

(c) On the same grid provided, draw triangles ABC and A"B"C".

(2 marks)



(d) Determine a single matrix that maps ABC onto A"B"C".

(2 marks)

ABC
$$\frac{NM}{(NM)^{-1}} \rightarrow A^{\parallel}B^{\parallel}C^{\parallel}$$

$$|QP M = \begin{pmatrix} 0 & 1 \\ 1 & -2 \end{pmatrix}, N = \begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix}$$

$$NM = \begin{pmatrix} -2 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 1 & -2 \end{pmatrix} = \begin{pmatrix} 0 & -2 \\ -1 & 2 \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 0 & -2 \\ -1 & 2 \end{pmatrix}$$

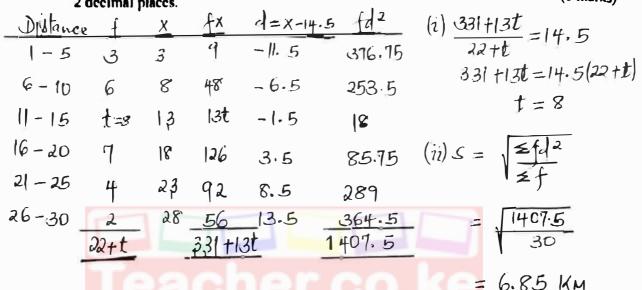


22. Workers in a factory commute from their homes to the factory. The table below shows the distances in kilometres, covered by the workers.

Distance (km)	1 - 5	6 – 10	H = 15	16 - 20	21 – 25	26 – 30
Number of workers	3	6	1	7	4	2

The mean distance covered was 14.5 km.

(a) Determine the value of t and hence the standard deviation of the distances correct to 2 decimal places. (6 marks)



(b) Calculate, correct to 2 decimal places, the interquartile range of the distances. (4 marks)

Distance			
1-5	3 3	41 - 4.00 - 1.0	
	6 9	- 77 - 71	9.25 KM
11-15	E 17	$Q_{3} = 3.80 = 22.5^{12}$	
16-20	7 24	4	
21 - 25	4 28	$= 15.5 + \left(\frac{22.5 - 17}{7}\right) \times 5$	=19.43 Km
	$\frac{2}{30}$ 30	$Q_3 - Q_1 = 19.43 - 9.25 =$	= 10.18 KM

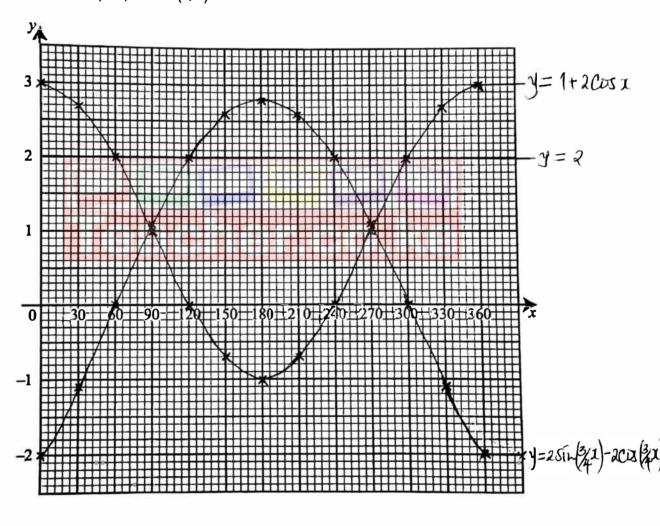


23. (a) Complete the table below giving the values correct to 1 decimal place.

x°	0	30	60	90	120	150	180	210	240	270	300	330	360
$y = 2\sin\left(\frac{3}{4}x\right) - 2\cos\left(\frac{3}{4}x\right)$	-2	-1.1	0	(11)	2	2.6	2.8	2.6) 2	1.1	0 ,	(-1.1)	-2
$y=1+2\cos x$	3	2.7)	2	1	0	-0.7	-1	-0:7	0	1	2	2.7	3

(2 marks)

(b) On the grid provided and using the same axis, draw the graphs of
$$y = 2\sin\left(\frac{3}{4}x\right) - 2\cos\left(\frac{3}{4}x\right)$$
 and $y = 1 + 2\cos x$ for $0^{\circ} \le x \le 360^{\circ}$. (4 marks)





Using the graphs in part (b): (c)

- find the values of x for which $\sin\left(\frac{3}{4}x\right) = 1 + \cos\left(\frac{3}{4}x\right)$. $y = 2 \left[S(u) \left(\frac{3}{4}x\right) Co(\frac{3}{4}x) \right]$ $\frac{1}{2} = \left[S(u) \left(\frac{3}{4}x\right) Co(\frac{3}{4}x) \right]$ (2 marks)
- determine the range of x for which $2\sin\left(\frac{3}{4}x\right) 2\cos\left(\frac{3}{4}x\right) > 1 + 2\cos x$. (ii)





- A particle was moving along a straight line. The acceleration of the particle after t seconds was given by (4t 13) ms⁻². The initial velocity of the particle was 18 ms⁻¹.
 - (a) Determine the value of t when the particle is momentarily at rest. (5 marks)

$$V = \int a dt$$

$$= \int (4t - 13) dt$$

$$= 2t^{2} - 13t + c$$
of initial valueity, $t = 0$, $V = 18 \Rightarrow c = i8$

$$V = 2t^{2} - 13t + 18$$

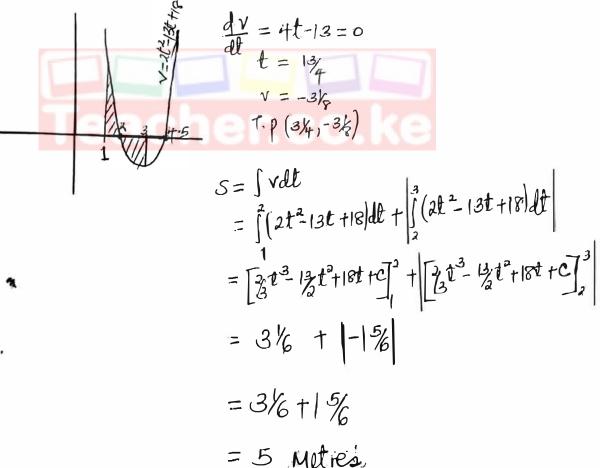
$$Dul V = 0 = 2t^{2} - 13t + 18$$

$$\Rightarrow (t - 2)(2t - 9) = 0$$

$$t - 2 = 0 \text{ or } 2t - 9 = 0$$

$$\Rightarrow t = 2 \text{ sec. or } t = 4.5 \text{ sec.}$$

(b) Find the distance covered by the particle between the time t = 1 second and t = 3 seconds. (5 marks)



THIS IS THE LAST PRINTED PAGE.