

2. Surds

<p>1.</p> $BC = \sqrt{r5^2 + 1^2}$ $\sin(90 - \theta) \frac{\sqrt{5}}{\sqrt{6}}$	<p>B1</p> <p>B1</p> <p>B1</p>	<p>02</p>
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$$1.. \quad \frac{3}{\sqrt{7}-2} + \frac{1}{\sqrt{7}} = \frac{3}{\sqrt{7}-2} \cdot \frac{7+2}{7+2} + \frac{\sqrt{7}}{\sqrt{7}}$$

$$\begin{aligned} & \frac{3}{\sqrt{7}-2} \cdot \frac{1 = 3\sqrt{7} + 7 - 2}{\sqrt{7}} \cdot \frac{7-2}{7} \\ & 3\sqrt{7} + (7-2) \\ & 7 - 2\sqrt{7} \\ & = \frac{3\sqrt{7} + 7 - 2}{7-2\sqrt{7}} \cdot \frac{7+2\sqrt{7}}{7+2\sqrt{7}} \\ & = 49 - 28 \\ & = \frac{(3\sqrt{7} + 7-2)(7+2\sqrt{7})}{21} \\ & = \frac{(4\sqrt{7}-2)(7+2\sqrt{7})}{21} \end{aligned}$$

2.

$$\frac{2+\sqrt{5}}{2-\sqrt{5}} - \frac{3+\sqrt{5}}{2+\sqrt{5}} = a + b\sqrt{5}$$

$$\frac{4+4\sqrt{5}+\sqrt{5}-(6-3\sqrt{5}+2\sqrt{5}-5)}{4-5}$$

$$\frac{8+5\sqrt{5}}{-1}$$

$$a = -8 \quad b = -5$$

3.

$$\frac{\sqrt{14}(\sqrt{7} + \sqrt{2}) - \sqrt{14}(\sqrt{7} - \sqrt{12})}{\sqrt{14} \cdot \sqrt{7} + \sqrt{14} \cdot \sqrt{12} - \sqrt{14} \cdot \sqrt{7} + \sqrt{14} \cdot \sqrt{12}}$$

$$\frac{7-12}{7-12}$$

-5

4.

$$(\sqrt{2-1})^2 = 2\sqrt{2-2} + 1 \cancel{\sqrt{3-2}} - 2$$

$$(\sqrt{2-1})^3 = 2 - 1(\cancel{\sqrt{3-2}}) - 2$$

$$= 5\sqrt{2-7}$$

$$\frac{2-\cancel{2}}{5\cancel{2-7}} \times \frac{5\cancel{2+7}}{5\cancel{2-7}} = 2\sqrt{2+7) - 2\sqrt{2+2)}$$

$$= 17\cancel{2-6} = -6 + 1\cancel{2}$$

5.

$$(2-3)(3+2)$$

$$3(2)2-2)2$$

$$\frac{3x2-3+2-2}{9x2-4x3}$$

$$\frac{6-3+2-6}{18-12}=6$$

6.

$$i) Or = 16^2 - 5^2$$

$$= \sqrt{256-25}$$

$$= 15.198 \text{ cm}$$

$$ii) \tan \theta = \frac{5.066}{4} = 1.2665$$

$$\therefore \theta = 51.71^\circ$$

7. $\log_{10} 5 - \log_{10} 10^2 + \log_{10} (2y + 10) = \log_{10} (y-4)$

$$\log_{10} \frac{5(2y+10)}{10^2} = \log_{10} (y-4)$$

$$10y + 50 = 100y - 400$$

$$90y = 450$$

$$y = 5$$

8.

$$\frac{\sqrt{3}-\sqrt{2}-\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}[\sqrt{3}-\sqrt{2}]}$$

$$= \frac{3-\sqrt{6}-\sqrt{6}+2}{3-\sqrt{6}+\sqrt{6}-2}$$

$$= \frac{5-2\sqrt{6}}{3-2}$$

$$= 5-2\sqrt{6}$$