

# 1. Surds

1. Given that  $\tan\theta = \frac{1}{\sqrt{5}}$  and  $\theta$  is an acute angle, find without using tables or calculators,  $\sin(90 - \theta)$ , leaving your answer in simplified surd form. (2mks)

2. Given that  $\sqrt{3} = 1.7321$ , express in surd form, rationalize the denominator and then find the value of the expression below to 5 significant figures without using the calculator. (3mks)

$$\frac{2 - \tan 60^\circ}{3 - 2 \cos 30^\circ}$$

3. Simplify  $(1 + \sqrt{3})(1 - \sqrt{3})$  and hence evaluate  $\frac{1}{1 + \sqrt{3}}$  to 3 significant figures given that  $\sqrt{3} = 1.7321$ . (3mks)

4. Without using mathematical tables or calculators, find the volume of a container whose base is a regular hexagon of side  $\sqrt{3}$  cm and height  $2\sqrt{3}$  cm (4 mks)

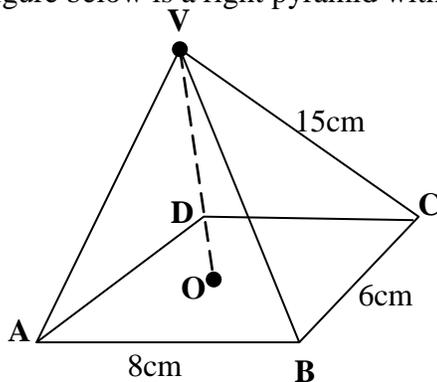
5. Simplify;  $\frac{3}{\sqrt{7} - 2} + \frac{1}{\sqrt{7}}$  leaving the answer in the form  $a + b\sqrt{c}$ , where  $a$ ,  $b$  and  $c$  are rational numbers

6. Given that:-  $\frac{2 + \sqrt{5}}{2 - \sqrt{5}} - \frac{3 + \sqrt{5}}{2 + \sqrt{5}} = a + b\sqrt{5}$   
Find the values of  $a$  and  $b$  where  $a$  and  $b$  are rational numbers

7. If:-  $\frac{\sqrt{4}}{\sqrt{7} - \sqrt{12}} - \frac{\sqrt{4}}{\sqrt{7} + \sqrt{2}} = a\sqrt{7} + b\sqrt{2}$  Find the values of  $a$  and  $b$ , where  $a$  and  $b$  are rational numbers \*

8. Rationalize the denominator  $\frac{2 - \sqrt{2}}{(\sqrt{2} - 1)^3}$  and express your answer in the form of  $a + c$

9. The figure below is a right pyramid with a rectangular base ABCD and vertex V.



O is the centre of the base and M is a point on OV such that  $OM = \frac{1}{3} OV$ ,  $AB = 8$  cm,  $BC = 6$  cm and  $VA = VB = VD = VC = 15$  cm. Find ;

- i) The height OV of the pyramid.  
ii) The angle between the plane BMC and base ABCD.
10. Find the value of  $y$  which satisfies the equation  
 $\log_{10} 5 - 2 + \log_{10} (2y + 10) = \log_{10} (y - 4)$

11. Simplify the expression  $\frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}}$  giving your answer in the form of  $a + b\sqrt{c}$ .