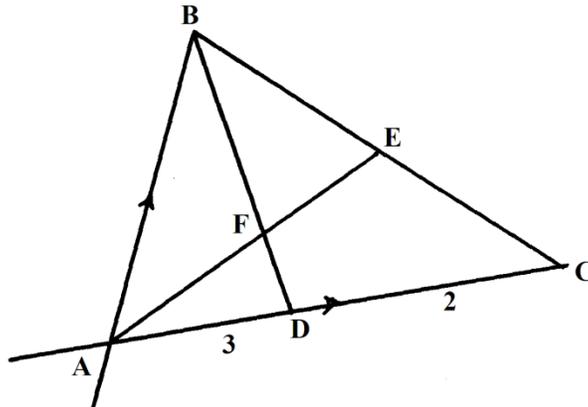


1. Vectors 2

1. In the figure below E is the mid point of BC. $AD:DC = 3:2$ and F is the meeting point of BD and AE



If $\vec{AB} = \vec{b}$ and $\vec{AC} = \vec{c}$

(a) Express the following in terms of \vec{b} and \vec{c}

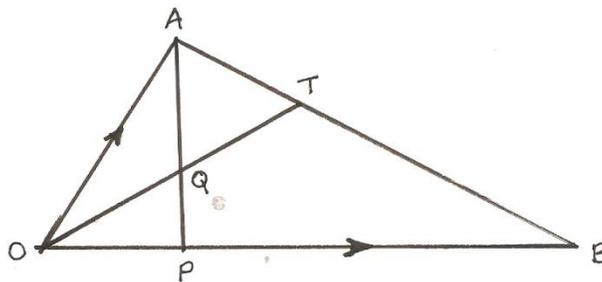
(i) \vec{BD} (1mk)

(ii) \vec{AE} (2mks)

(b) If $\vec{BF} = t\vec{BD}$ and $\vec{AF} = n\vec{AE}$ find the value of t and n. (5mks)

(c) State the ratio of BD to BF. (1mk)

2. In the figure below $\vec{OA} = \vec{a}$ and $\vec{OB} = \vec{b}$. Points P and T divide \vec{OB} and \vec{AB} internally in the ration 2:3 and 1:3 respectively. Lines \vec{OT} and \vec{AP} meet at Q.



Find in terms of \vec{a} and \vec{b}

(i) \vec{OT} (3mks)

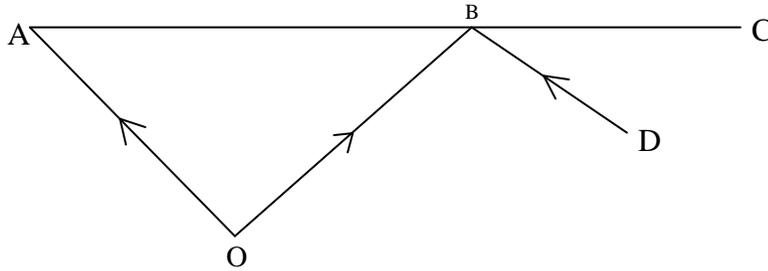
(ii) \vec{OP} (1mk)

(iii) \vec{AP} (1mk)

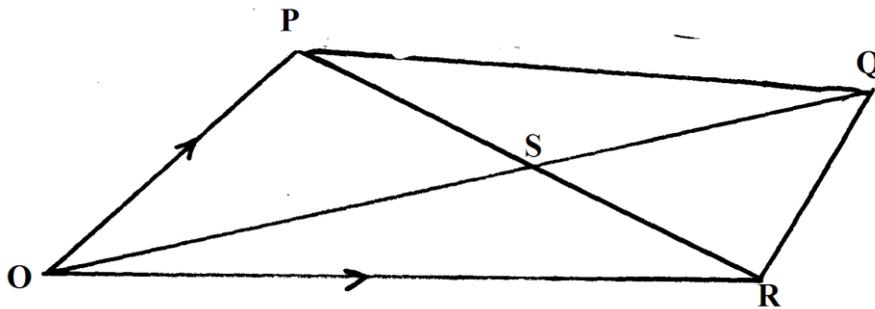
(iv) \vec{OQ} (5mks)

If $\vec{OQ} = k\vec{OT}$ and $\vec{AQ} = h\vec{AP}$ where k and h are constants express OQ in two different ways and hence find the values of h and k. (10mks)

3. In the figure below $\underline{OA} = \underline{a}$, $\underline{OB} = \underline{b}$ and DB is parallel to OA. C is on AB extended such that $AB:BC = 2:1$ and that $OA = 3DB$.



- a) Express the vector BC in terms of \underline{a} and \underline{b} . (1mk)
- b) Show by vector methods that the points O, D and C are collinear. (3mks)
4. In the figure below $\vec{OP} = \frac{1}{2}\underline{a} + \underline{b}$, $\vec{OR} = \frac{7}{2}\underline{a} - \underline{b}$, $\vec{RQ} = \frac{3}{2}k\underline{b} + \frac{1}{2}m\underline{a}$, where k and m are scalars 2PS
= 3SR.



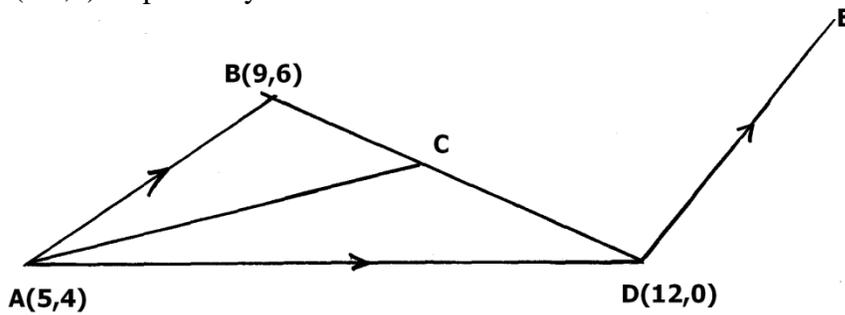
(a) Express as simply as possible in terms of \underline{a} and \underline{b} each of the following vectors.

- (i) \vec{PR} (1mk)
- (ii) \vec{PS} (1mk)
- (iii) \vec{OS} (1mk)

(b) Express \vec{OQ} in terms of a, b, k and m. (2mks)

(c) If Q lies on \vec{OS} produced with $\vec{OQ}; \vec{OS} = 5:4$, find the value of k and m. (5mks)

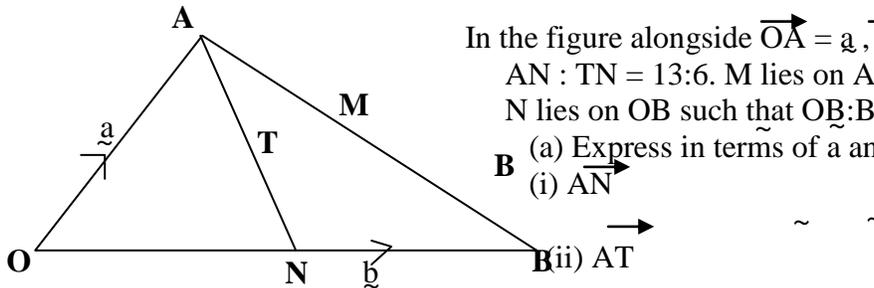
5. In the figure below, $DE = \frac{1}{2} AB$ and $BC = \frac{2}{3} BD$ and the co ordinates of A,B and D are (5,4), (9,6) and (12,0) respectively.



Find the vectors

- (i) \vec{BD} (1mk)
 (ii) \vec{BC} (1mk)
 (iii) \vec{CD} (1mk)
 (iv) \vec{AC} (2mks)
- b) Given that $AC = kCE$; where k is a scalar,
 Find
- (i) the value of k (4mks)
 (ii) the ratio in which C divide AE . (1mk)

6. In the figure alongside $\vec{OA} = \vec{a}$, $\vec{OB} = \vec{b}$. T lies on AN such that $AN : TN = 13:6$. M lies on AB such that $\vec{AM} : \vec{MB} = 1:3$ and N lies on OB such that $\vec{ON} : \vec{NB} = 7:-5$.



- (a) Express in terms of \vec{a} and \vec{b} in the simplest form
- (i) \vec{AN}

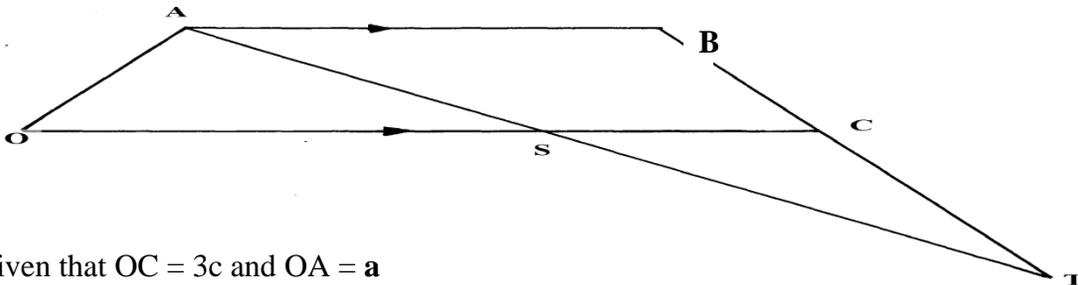
- (ii) \vec{AT}
- (iii) \vec{AM}
- (b) Show that O , T and M are collinear and state the ratio of $OT : TM$

7. A point $(-3, 4)$ divides \vec{AB} internally in the ratio $3:5$. Find the coordinates of point A given that point B is $(6, -5)$

8. Given that O is the origin, $\vec{OA} = 3\vec{i} + 2\vec{j} - 4\vec{k}$ and $\vec{OB} = 6\vec{i} + 11\vec{j} + 2\vec{k}$. If x divides AB in the ratio $1:2$, find the modulus of \vec{OX} to 2d.p

9. a) Expand $(2 - \frac{1}{5}x)^5$
 b) Hence use the expansion to find the value of $(1.96)^5$ correct to 3 decimal places

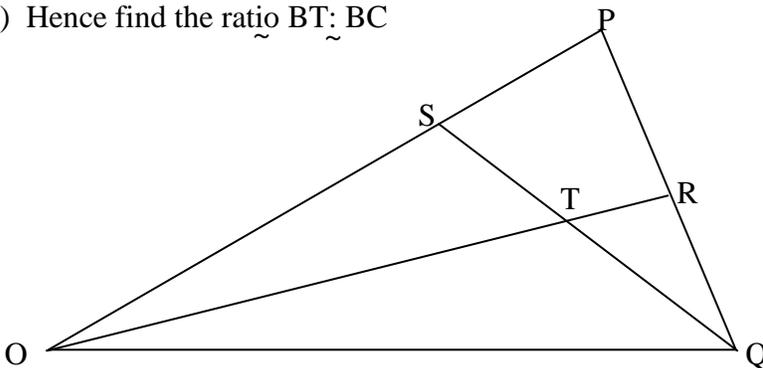
10. In the figure OABC is a trapezium in which $3 \vec{AB} = 2\vec{OC}$. S divides OC in the ratio 2:1 and AS produced meets BC produced at T



Given that $OC = 3c$ and $OA = \mathbf{a}$

- Express AS and BC in terms of \mathbf{a} and \mathbf{c}
- Given further that $AT = h\vec{AS}$ and $\vec{BT} = k\vec{BC}$ where h and k are constants
 - Express AT in two ways in terms \mathbf{a} , \mathbf{c} , h and k
- The obtuse angle between the lines PQ
- Hence find the ratio $BT:BC$

11.



In the figure above, OPQ is a triangle in which $OS = \frac{3}{4} OP$ and $PR:RQ = 2:1$. Lines OR and SQ meet at T.

- Given that $OP = \mathbf{p}$ and $OQ = \mathbf{q}$, express the following vectors in term of \mathbf{p} and \mathbf{q}
 - PQ
 - OR
 - SQ
- You are further given that $ST = m \vec{SQ}$ and $OT = n \vec{OR}$. Determine the values of m and n